

Fregean Semantics: Denotation (reference)

All linguistic expressions (proper names, predicates, sentences) denote **objects**.

- The denotation of a proper name is an **individual**.
- The denotation of a predicate is a **function** (which maps one object as *argument* to another object as *value*).
- The denotation of a sentence is a **truth-value**.
- A **concept** is a function whose values are truth-values.

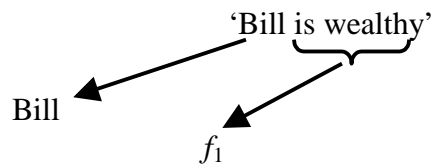
Example: 'Bill is wealthy'

'Bill' denotes Bill.

'is wealthy' denotes a function, f_1 .

$\text{Bill} = \mathbf{D}(\text{'Bill'})$

$f_1 = \mathbf{D}(\text{'is wealthy'})$



f_1 maps individuals onto truth-values:
That is, f_1 maps Bill onto The True.

$f_1(\text{Bill}) = \text{The True}$

$\mathbf{D}(\text{'Bill is wealthy'})$ is a function of $\mathbf{D}(\text{'Bill'})$ and $\mathbf{D}(\text{'is wealthy'})$.

$\mathbf{D}(\text{'Bill is wealthy'}) = \text{The True}$

The denotation of the entire sentence is a function of the denotations of its parts.

Example: 'Bill loves Melinda'

'Bill' denotes Bill.

'Melinda' denotes Melinda.

'loves' denotes a function, f_2 .

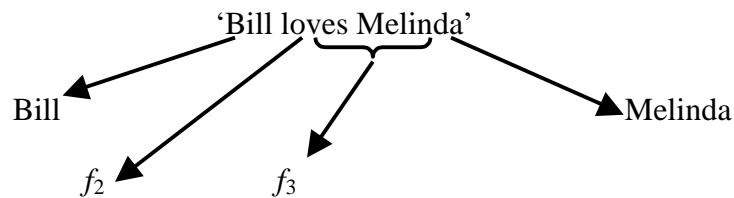
'loves Melinda' denotes a function, f_3 .

$\text{Bill} = \mathbf{D}(\text{'Bill'})$

$\text{Melinda} = \mathbf{D}(\text{'Melinda'})$

$f_2 = \mathbf{D}(\text{'loves'})$

$f_3 = \mathbf{D}(\text{'loves Melinda'})$



f_2 maps individuals onto functions:
That is, f_2 maps Melinda onto f_3 .

$f_2(\text{Melinda}) = f_3$

f_3 maps individuals onto truth-values:
That is, f_3 maps Bill onto The True.

$f_3(\text{Bill}) = \text{The True}$

$\mathbf{D}(\text{'Bill loves Melinda'})$ is a function of $\mathbf{D}(\text{'Bill'})$, $\mathbf{D}(\text{'Melinda'})$, and $\mathbf{D}(\text{'loves'})$.

$\mathbf{D}(\text{'Bill loves Melinda'}) = \text{The True}$

Again, the denotation of the entire sentence is a function of the denotations of its parts.

Fregean Semantics: Sense

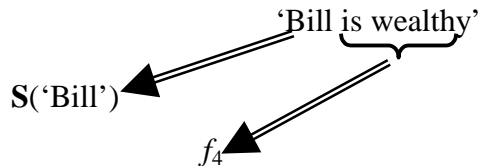
All linguistic expressions (proper names, predicates, sentences) express **senses**.

- The sense of a predicate is a **function** from a sense to a sense.
- The sense of a sentence is a **thought** (i.e., a proposition).

Example: 'Bill is wealthy'

'Bill' expresses $S('Bill')$.

'is wealthy' expresses a function, f_4 . $f_4 = S('is\ wealthy')$



f_4 maps senses onto thoughts: $f_4(S('Bill')) = S('Bill\ is\ wealthy')$

That is, f_4 maps $S('Bill')$ onto the sense of 'Bill is wealthy'.

$S('Bill\ is\ wealthy')$ is the *thought*, or proposition, that Bill is wealthy.

$S('Bill\ is\ wealthy')$ is a function of $S('Bill')$ and $S('is\ wealthy')$.

That is, the sense of the entire sentence is a function of the senses of its parts.

Example: 'Bill loves Melinda'

'Bill' expresses $S('Bill')$.

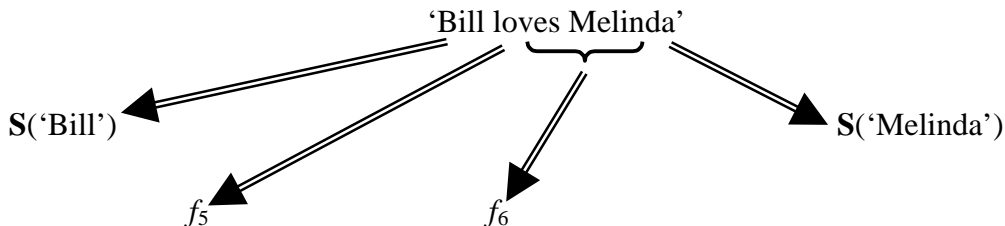
'Melinda' expresses $S('Melinda')$.

'loves' expresses a function, f_5 .

'loves Melinda' expresses a function, f_6 .

$f_5 = S('loves')$

$f_6 = S('loves\ Melinda')$



f_5 maps senses onto functions: $f_5(S('Melinda')) = f_6$.

That is, f_5 maps $S('Melinda')$ onto f_6 , the function that is the sense of 'loves Melinda'.

f_6 maps senses onto thoughts: $f_6(S('Bill')) = S('Bill\ loves\ Melinda')$

That is, f_6 maps $S('Bill')$ onto the thought that Bill loves Melinda.

$S('Bill\ loves\ Melinda')$ is a function of $S('Bill')$, $S('Melinda')$, and $S('loves')$.

That is, the sense of the entire sentence is a function of the senses of its parts.