

**Homework #9 due Tonight**

**Hour exam Friday, Nov 30 -- Material in Ch 9, 10, and 11 through 11.2. Understanding 11.3 might not hurt. (also Tutorial and Lab as usual)**

**Office hrs today 4-5:30 and tomorrow 4-5:30.**

**CLUE exam review tonight at 7pm in Mary Gates Hall 254**

**Final homework assignment due Friday Dec 7**

**MASS** – why is **gravity mass** and **inertia mass** the same? Or is it? **Experimental**

$$F_g = GMm/r^2 = ma \text{ same } m.$$

Consequence – different materials fall the same, or equivalently, don't need a different  $G$  for each kind of stuff.

Best experiments with **torsion pendulums**, compare attraction of source masses to different material test masses.  $\Delta a/a < 2 \times 10^{-13}$  done here at UW by Adelberger, Heckel, Gundlach.

**“The equivalence principle”** – basis for general relativity.

**Gravitational potential energy:** We will treat the special case of a big object attracting a small one. So C.M. of system is approx at center of large object.

Small one located at  $r$  from the center of the big one. ( $r$  for gravity and  $r$  to cm are same.)

$$U(r) = - \int_{r_0}^r \vec{F} \cdot d\vec{r} = - \int_{r_0}^r \left( \frac{-GMm}{r^2} \hat{r} \right) \cdot d\vec{r}$$

$$= GMm \int_{r_0}^r \frac{dr}{r^2} = GMm(-1/r + 1/r_0)$$

Pick constant  $r_0$  so  **$U \rightarrow 0$  as  $r \rightarrow \infty$**

That is  $r_0 = \infty$  Then  $U(r) = -GMm / r$

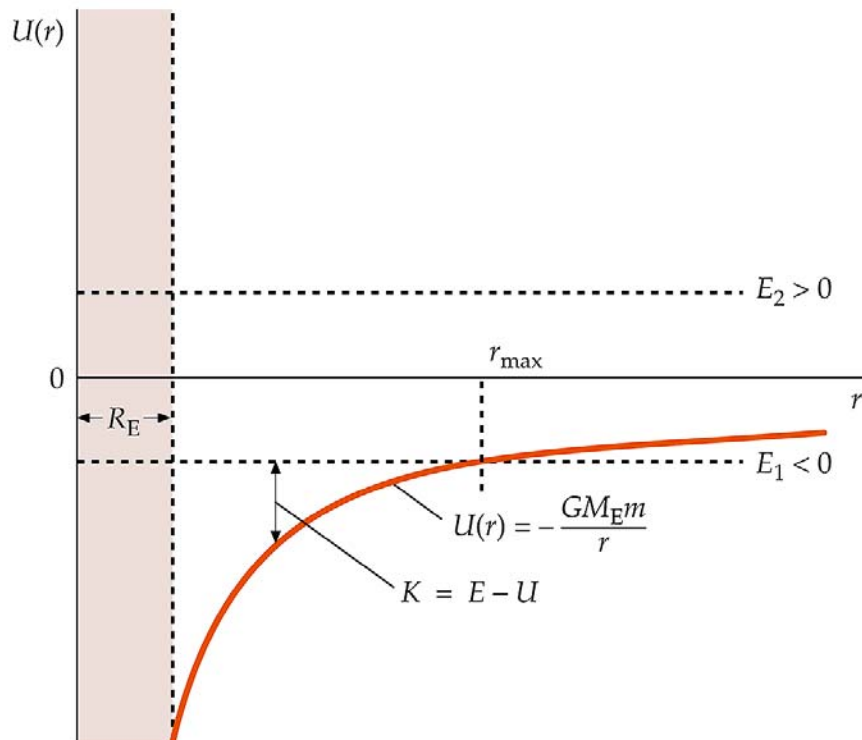
Show  $U(R_E + h) = U(R_E) + mgh$

**Binding energy:** Object at rest at, say,  $R_E$  has negative energy. If you add an equal magnitude of positive energy, the object could be free, with net energy 0. **Bound things have  $E < 0$ .**

**Escape velocity:**  $v_{\text{esc}}$  (in the  $\hat{r}$  direction)  
so  $\frac{1}{2} m v_{\text{esc}}^2 = GM_E m / R_E$  for object on surface of Earth. (or appropriate  $M$  and  $R$  for other thing.)

$$GM_E / R_E^2 = g \quad \text{so} \quad v_{\text{esc}}^2 = 2g R_E \rightarrow$$

$$v_{\text{esc}} = \sqrt{2(9.8)(6.4 \times 10^6)} \approx 11 \text{ km/s}$$



For gravity from complicated objects, we can define the **Gravitational Field** (works for simple objects too.)

What is **force on a unit mass**?  $\vec{g} = \vec{F}_g / m$

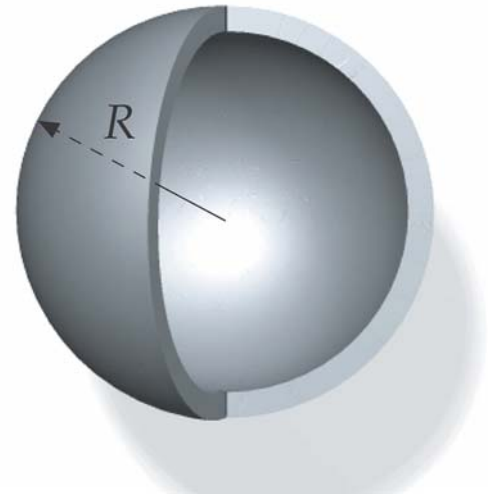
This is just the acceleration.

If the field comes from several masses, the **fields** from each **sum**:  $\vec{g} = \sum_i \vec{g}_i$  or  $\vec{g} = \int d\vec{g}$

In 11.5 the derivation is done showing, for a shell of mass  $M$ , radius  $R$ , centered at the origin, the field is

1.  **$\vec{g}(r)=0$**  if you are **inside** the shell

2.  **$\vec{g}(r) = -\frac{GM}{r^2} \hat{r}$**  **outside.**



So outside it looks like a point mass at the origin.

Thus a sphere also looks like a point mass at the origin from outside, as long as the density only depends on  $r$ . (think of an onion)

Inside you get field from the sphere contained within the radius you are at.

## **SUMMARY of material covered since last exam**

**Ch 9 – Rotational motion.**

**Angular coordinates, velocity, acceleration.**

**Moment of inertia and Torque**

**See table 9-2 for analogs.**

**Rolling without (then with) slipping.**

**Ch 10 – Polar vectors and angular momentum**

**Vector products (cross products) for torque and angular momentum.**

**Conservation of angular momentum – collisions where angular momentum is conserved.**

**Newton's law for torques and angular momentum in vector form. – The gyroscope**

**(Skipped 10-4, quantization of angular momentum)**

**Ch 11 – Gravity: Kepler's laws, Newton's law of gravity. Orbits of various sorts. (also 11.3-5, which will not be on the coming exam.)**