## AMath 483/583 - Lecture 3

This lecture:

- computing square roots
- Python demo
- git demo


## Reading:

- class notes: git section
- class notes: Python sections (new)


## Computing square roots

Hardware arithmetic units can add, subtract, multiply, divide.
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Example: Compute $\sqrt{2} \approx 1.4142135623730951$
In most languages, sqrt(2) computes this.

```
>>> from numpy import sqrt
>>> sqrt(2.)
```


## One possible algorithm to approximate $s=\sqrt{x}$

```
s = 1. # or some better initial guess
for k in range(kmax):
    s}=0.5* (s+x/s
```

where kmax is some maximum number of iterations.
Note: In Python, range(N) is $[0,1,2,, \ldots, N-1]$.

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In fact this is Newton's method to find root of $s^{2}-x=0$.

## Newton's method

Problem: Find a solution of $f(s)=0$ (zero or root of $f$ )

Idea: Given approximation $s^{[k]}$, approximate $f(s)$ by a linear function, the tangent line at $\left(s^{[k]}, f\left(s^{[k]}\right)\right)$.
Find unique zero of this function and use as $s^{[k+1]}$.

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Updating formula:

$$
s^{[k+1]}=s^{[k]}-\frac{f\left(s^{[k]}\right)}{f^{\prime}\left(s^{[k]}\right)}
$$

## Demo...

Goals:

- Develop our own version of sqre function.
- Start simple and add complexity in stages.
- Illustrate some Python programming.
- Illustrate use of git to track our development

We will do this in \$UWHPSC/lectures/lecture3 directory so you can examine the various versions later.

