AMath 483/583 — Lecture 17

Outline:

- Fine grain vs. coarse grain parallelism
- Manually splitting loops between threads
- Examples with bugs

Reading:

- class notes: OpenMP section of Bibliography
- `$UWHPSC/codes/openmp`
- **`https://computing.llnl.gov/tutorials/openMP/`**

Fine vs. coarse grain parallelism

Fine grain: Parallelize at the level of individual loops, splitting work for each loop between threads.

Coarse grain: Split problem up into large pieces and have each thread deal with one piece.

May need to synchronize or share information at some points.

Fine vs. coarse grain parallelism

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More similar to what must be done in MPI.

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Domain Decomposition: Splitting up a problem on a large domain (e.g. three-dimensional grid) into pieces that are handled separated (with suitable coupling).

Solution of independent ODEs by Euler's method

Solve $u_i'(t) = c_i u_i(t)$ for $t \geq 0$
with initial condition $u_i(0) = \eta_i$.

Decoupled system of ODEs for $i = 1,\ 2,\ \ldots,\ n$

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Decoupled system of ODEs for $i = 1,\ 2,\ \ldots,\ n$

Exact solution: $u_i(t) = e^{c_i t}\eta_i$.

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Exact solution: $u_i(t) = e^{c_i t}\eta_i$.

Euler method: $u_i(t + \Delta t) \approx u_i(t) + \Delta t c_i u_i(t) = (1 + c_i \Delta t)u_i(t)$.

Implement this for large number of time steps for large n.

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Implement this for large number of time steps for large n.

For each i time stepping can't be easily made parallel.

But for large n, this problem is embarassingly parallel:

Problem for each i is completely decoupled from problem for any other i. Could solve them all simultaneously with no communication needed.

Fine grain solution with parallel do loops

```
!$omp parallel do
do i=1,n
    u(i) = eta(i)
    enddo

do m=1,nsteps
    !$omp parallel do
    do i=1,n
        u(i) = (1.d0 + dt*c(i))*u(i)
        enddo
    enddo
```

Note that threads are forked `nsteps+1` times.

Requires shared memory:

don't know which thread will handle each `i`.

Fine grain solution with parallel do loops

Might try to fork threads only once via: Wrong!

```
!$omp parallel private(m)
!$omp do
do i=1,n
    u(i) = eta(i)
    enddo

do m=1,nsteps
    !$omp do
    do i=1,n
        u(i) = (1.d0 + dt*c(i))*u(i)
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    enddo
!$omp end parallel
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    enddo
!$omp end parallel
```

Error: the loop on m will be done independently by each thread.
(Actually works in this case but not good coding.)

Fine grain solution with parallel do loops

Can rearrange loops:

```
!$omp parallel private(m)
!$omp do
do i=1,n
    u(i) = eta(i)
    enddo

!$omp do
do i=1,n
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        u(i) = (1.d0 + dt*c(i))*u(i)
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        u(i) = (1.d0 + dt*c(i))*u(i)
        enddo
    enddo
!$omp end parallel
```

Only works because ODEs are decoupled — can take all time steps on $u_1(t)$ without interacting with $u_2(t)$, for example.

Coarse grain solution of ODEs

Split up $i = 1, 2, \ldots, n$ into `nthreads` disjoint sets.

A set goes from `i=istart` to `i=iend`

These private values are different for each thread.

Each thread handles 1 set for the entire problem.

```
!$omp parallel private(istart,iend,i,m)

istart = ??
iend = ??

do i=istart,iend
    u(i) = eta(i)
    enddo

do m=1,nsteps
    do i=istart,iend
        u(i) = (1.d0 + dt*c(i))*u(i)
        enddo
    enddo
!$omp end parallel
```

Threads are forked only once,

Each thread only needs subset of data.

Setting `istart` and `iend`

Example: If `n=100` and `nthreads = 2`, we would want:

Thread 0: `istart= 1` and `iend= 50`,
Thread 1: `istart=51` and `iend=100`.

If `nthreads` divides `n` evenly...

```
points_per_thread = n / nthreads

!$omp parallel private(thread_num, istart, iend, i)

    thread_num = 0      ! needed in serial mode
    !$ thread_num = omp_get_thread_num()

    istart = thread_num * points_per_thread + 1
    iend = (thread_num+1) * points_per_thread

    do i=istart,iend
        ! work on thread's part of array
        enddo
    ...

!$omp end parallel
```

Setting `istart` and `iend` more generally

Example: If `n=101` and `nthreads = 2`, we would want:

Thread 0: `istart= 1` and `iend= 51`,
Thread 1: `istart=52` and `iend=101`.

If `nthreads` might not divide `n` evenly...

```
points_per_thread = (n + nthreads - 1) / nthreads

!$omp parallel private(thread_num, istart, iend, i)

    thread_num = 0      ! needed in serial mode
    !$ thread_num = omp_get_thread_num()

    istart = thread_num * points_per_thread + 1
    iend = min((thread_num+1) * points_per_thread, n)

    do i=istart,iend
        ! work on thread's part of array
        enddo
    ...

!$omp end parallel
```

Example: Normalizing a vector

Given a vector (1-dimensional array) x,
Compute the normalized vector $x/\|x\|_1$, with $\|x\|_1 = \sum_{i=1}^{n} |x_i|$

Fine-grain: Using `parallel do` loops.

```
norm = 0.d0
!$omp parallel do reduction(+ : norm)
do i=1,n
    norm = norm + abs(x(i))
    enddo

!$omp parallel do
do i=1,n
    x(i) = x(i) / norm
    enddo
```

Note: Must finish computing `norm` before using for any `x(i)`, so we are using the implicit barrier after the first loop.

Example: Normalizing a vector

Another fine-grain approach, forking threads only once:

```
! from $UWHPSC/codes/openmp/normalize1.f90
    norm = 0.d0
    !$omp parallel private(i)

    !$omp do reduction(+ : norm)
    do i=1,n
        norm = norm + abs(x(i))
        enddo
    !$omp barrier  ! not needed (implicit)

    !$omp do
    do i=1,n
        x(i) = x(i) / norm
        enddo
    !$omp end parallel
```

Example: Normalizing a vector

Compute the normalized vector $x/\|x\|_1$, with $\|x\|_1 = \sum_{i=1}^{n} |x_i|$

Coarse grain version:

Assign blocks of i values to each thread. Threads must:

- Compute thread's contribution to $\|x\|_1$,

$$\texttt{norm\_thread} = \sum_{\texttt{istart}}^{\texttt{iend}} |x_i|,$$

- Collaborate to compute total value $\|x\|_1$:

$$\|x\|_1 = \sum_{\text{threads}} \texttt{norm\_thread}$$

- Loop over `i = istart, iend` to divide x_i by $\|x\|_1$.

Example: Normalizing a vector

```
! from $UWHPSC/codes/openmp/normalize2.f90

    norm = 0.d0
    !$omp parallel private(i,norm_thread, &
    !$omp                  istart,iend,thread_num)
    !$ thread_num = omp_get_thread_num()
    istart = thread_num * points_per_thread + 1
    iend = min((thread_num+1) * points_per_thread, n)

    norm_thread = 0.d0
    do i=istart,iend
        norm_thread = norm_thread + abs(x(i))
        enddo

    ! update global norm with value from each thread:
    !$omp critical
      norm = norm + norm_thread
    !$omp end critical

    !$omp barrier  !! needed here

    do i=istart,iend
        y(i) = x(i) / norm
        enddo

    !$omp end parallel
```

Example: Normalizing a vector — parallel block

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norm_thread = 0.d0
do i=istart,iend
    norm_thread = norm_thread + abs(x(i))
    enddo

! update global norm with value from each threa
!$omp critical
  norm = norm + norm_thread
!$omp end critical

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do i=istart,iend
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    enddo
```

Normalizing a vector — possible bugs

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Ok if it's in a `omp single` block. Otherwise second thread might set to zero after first thread has updated by `norm_thread`.

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3. Not using `omp critical` block to update global `norm`.

Data race.

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4. Not having a `barrier` between updating norm and using it.

First thread may use `norm` before other threads have added their contributions.

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4. Not having a `barrier` between updating norm and using it.

First thread may use `norm` before other threads have added their contributions.

None of these bugs would give compile or run-time errors!
Just wrong results (sometimes).

OpenMP example with shared exit criterion

Solve $u_i'(t) = c_i u_i(t)$ for $t \geq 0$
with initial condition $u_i(0) = \eta_i$.

Exact solution: $u_i(t) = e^{c_i t}\eta_i$.

Euler method: $u_i(t + \Delta t) \approx u_i(t) + \Delta t c_i u_i(t) = (1 + c_i \Delta t)u_i(t)$.

New wrinkle: Stop time stepping when any of the $u_i(t)$ values exceeds 100.

(Will certainly happen as long as $c_j > 0$ for some j.)

OpenMP example with shared exit criterion

Stop time stepping when any of the $u_i(t)$ values exceeds 100.

Idea:

Each time step, compute `umax` = maximum value of u_i over all i and exit the time-stepping if `umax > 100`.

OpenMP example with shared exit criterion

Stop time stepping when any of the $u_i(t)$ values exceeds 100.

Idea:

Each time step, compute `umax` = maximum value of u_i over all i and exit the time-stepping if `umax > 100`.

Each thread has a private variable `umax_thread` for the maximum value of u_i for its values of `i`. Updated for each `i`.

OpenMP example with shared exit criterion

Stop time stepping when any of the $u_i(t)$ values exceeds 100.

Idea:

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Each thread has a private variable `umax_thread` for the maximum value of u_i for its values of `i`. Updated for each `i`.

Each thread updates shared `umax` based on its `umax_thread`.
This needs to be done in critical section.

OpenMP example with shared exit criterion

Stop time stepping when any of the $u_i(t)$ values exceeds 100.

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This needs to be done in critical section.

Also need two barriers to make sure all threads are in synch at certain points.

OpenMP example with shared exit criterion

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This needs to be done in critical section.

Also need two barriers to make sure all threads are in synch at certain points.

Study code in `$UWHPSC/codes/openmp/umax1.f90`.

OpenMP example with shared exit criterion

```
!$omp parallel private(i,m,umax_thread, &
!$omp                  istart,iend,thread_num)
!$ thread_num = omp_get_thread_num()
istart = thread_num * points_per_thread + 1
iend = min((thread_num+1) * points_per_thread, n)

do m=1,nsteps
    umax_thread = 0.d0
    !$omp single
      umax = 0.d0
    !$omp end single
    do i=istart,iend
        u(i) = (1.d0 + c(i)*dt) * u(i)
        umax_thread = max(umax_thread, u(i))
        enddo

    !$omp critical
      umax = max(umax, umax_thread)
    !$omp end critical
    !$omp barrier

    if (umax > 100) exit
    !$omp barrier
    enddo
!$omp end parallel
```

do loop in parallel block:

```
do m=1,nsteps
    umax_thread = 0.d0
    !$omp single
      umax = 0.d0
    !$omp end single
    do i=istart,iend
        u(i) = (1.d0 + c(i)*dt) * u(i)
        umax_thread = max(umax_thread, u(i))
        enddo
    !$omp critical
      umax = max(umax, umax_thread)
    !$omp end critical
    !$omp barrier
    if (umax > 100) exit
    !$omp barrier
    enddo
```

OpenMP example with shared exit criterion

If there were **no** barriers, the following could happen:

Thread 0 executes critical section first, setting `umax` to 0.5.
Thread 0 checks if `umax > 100`. False, starts next iteration.
Thread 1 executes critical section, updating `umax` to 110.
Thread 1 checks if `umax > 100`. True, so it exits.
Thread 0 next sets `umax` to 0.4.

Thread 0 might never reach `umax > 100`. Runs forever.

OpenMP example with shared exit criterion

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Thread 0 executes critical section first, setting `umax` to 0.5.
Thread 0 checks if `umax > 100`. False, starts next iteration.
Thread 1 executes critical section, updating `umax` to 110.
Thread 1 checks if `umax > 100`. True, so it exits.
Thread 0 next sets `umax` to 0.4.

Thread 0 might never reach `umax > 100`. Runs forever.

With only first barrier, the following could happen:

`umax < 100` in iteration m.
Thread 1 checks if `umax > 100`. Go to iteration $m + 1$.
Thread 1 does iteration on i and sets `umax > 100`,
Stops at first barrier.
Thread 0 (iteration m) checks if `umax > 100`. True, Exits.

Thread 0 never reaches first barrier again, code hangs.