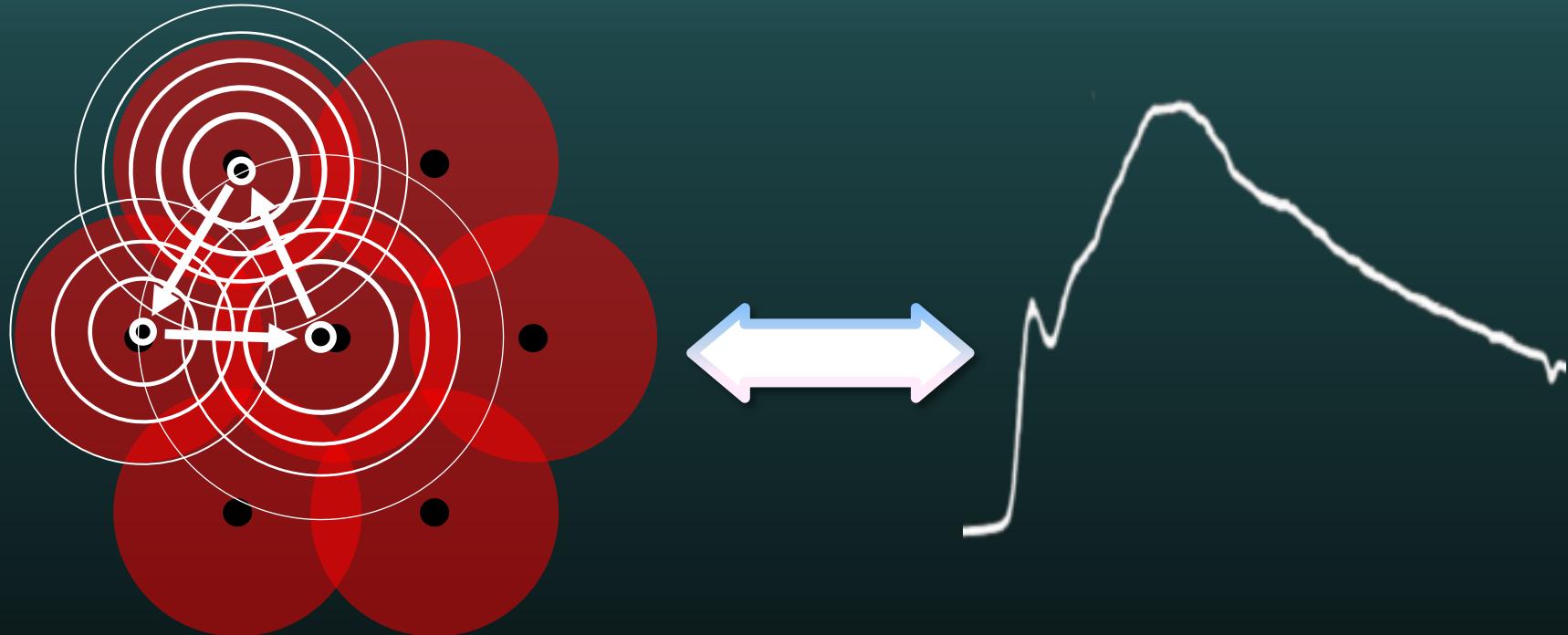


# Theory and Parameter Free Calculations of EELS and X-ray Spectra



J.J. Rehr<sup>1</sup>, J. J. Kas<sup>1</sup>, K. Jorissen<sup>2</sup>, and F. Vila<sup>1</sup>

<sup>1</sup>Department of Physics, University of Washington, <sup>2</sup>Amazon Web Services  
Seattle, WA

# Theory and Parameter Free Calculations of EELS and X-ray Spectra

- **GOAL:** Ab initio theory & interpretation of core level EELS & XAS

IR → VIS → UV → X-ray



- **TALK:** Advanced Codes & Workflow tools

Theory: FEFF/Green's function + OCEAN/BSE

If I can't calculate it,

I don't understand it.

(Often attributed to R. P. Feynman)

# Challenge:

## Full spectrum electron- and X-ray spectra

DEUTSCHES ELEKTRONEN-SYNCHROTRON

DESY

DESY SR-74/7  
May 1974

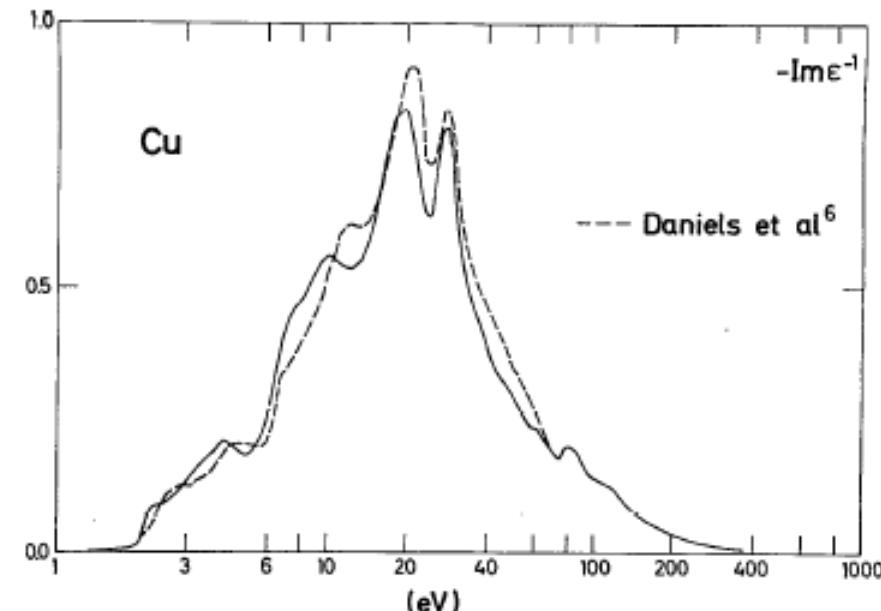
May 1974

Optical Constants from the Far Infrared to the X-Ray Region:

Mg, Al, Cu, Ag, Au, Bi, C, and  $\text{Al}_2\text{O}_3$

by

H.-J. Hagemann, W. Gudat, and C. Kunz



Cu loss function

# Challenge:

## Improve on Hydrogenic model of EELS\*

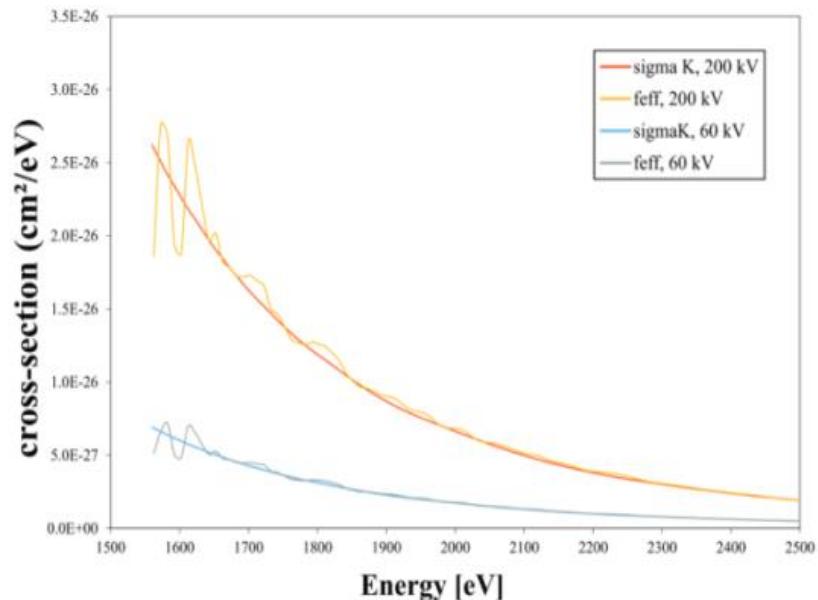
Ultramicroscopy 4 (1979) 169–179  
© North-Holland Publishing Company

### K-SHELL IONIZATION CROSS-SECTIONS FOR USE IN MICROANALYSIS

R.F. EGERTON

*Physics Department, University of Alberta, Edmonton, Canada, T6G 2J1*

Received 17 October 1978; in revised form 21 November 1978



L. Konrad *et al.*, MCM2015

\*L. Pauling, Proc. Roy Soc. A London 114, 181 (1927)

# $\sim$ 35 years later: *Ab initio* optical constants\*

PHYSICAL REVIEW B 80, 155110 (2009)

## Real space calculation of optical constants from optical to x-ray frequencies

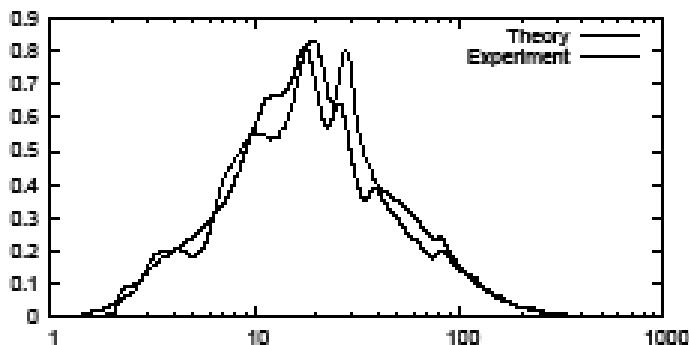
M. P. Prange,<sup>1</sup> J. J. Rehr,<sup>1</sup> G. Rivas,<sup>2</sup> J. J. Kas,<sup>1</sup> and John W. Lawson<sup>3</sup>

<sup>1</sup>*Department of Physics, University of Washington, Seattle, Washington 98195, USA*

<sup>2</sup>*Instituto de Ingeniería y Tecnología, Universidad Autónoma de Ciudad Juárez, Juárez 32310, Mexico*

<sup>3</sup>*NASA Ames Research Center, Mail Stop 229-1, Moffett Field, California 94035, USA*

(Received 17 October 2008; revised manuscript received 20 July 2009; published 5 October 2009)



Cu loss function

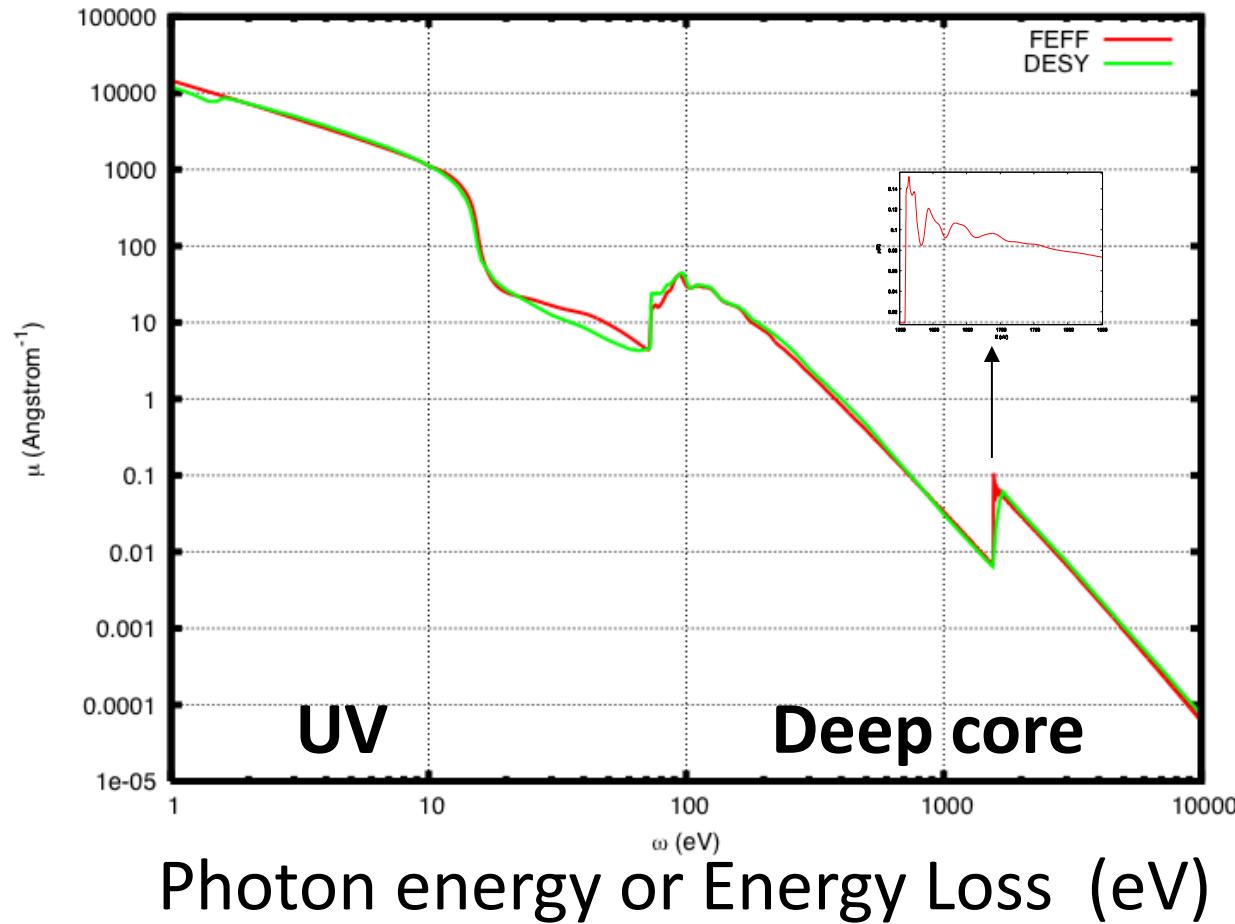
$\omega$ (eV)	$\epsilon_1$	$\epsilon_2$	n
.380000E+01	-.966246E+00	.492160E+01	.574110E+00
.390000E+01	-.874007E+00	.488653E+01	.583407E+00
.400000E+01	-.792192E+00	.485292E+01	.591411E+00
.410000E+01	-.725534E+00	.482128E+01	.597428E+00
.420000E+01	-.673854E+00	.479077E+01	.601251E+00
.430000E+01	-.631718E+00	.475174E+01	.602230E+00
.450000E+01	-.564064E+00	.467822E+01	.602254E+00
.475000E+01	-.527798E+00	.459519E+01	.595553E+00
.500000E+01	-.570524E+00	.447607E+01	.569409E+00
.550000E+01	-.597635E+00	.414935E+01	.511810E+00
.600000E+01	-.627088E+00	.377460E+01	.443231E+00

\*<http://feffproject.org/feff/desy>

# Optical constants

Dielectric function	$\epsilon = \epsilon_1 + i\epsilon_2$
<b>Energy Loss (EELS)</b>	$-\text{Im } \epsilon^{-1}$
Absorption coefficient	$\mu$
Refractive index	$n + i k$
Reflectivity	$R$
X-ray scattering factors	$f = f_0 + f_1 + i f_2$
Hamaker constants	$\epsilon(i\omega)$

# Broad Spectrum Calculations: Theory vs. Expt.



# EELS Theory *a lá* Fermi's golden rule

$$\frac{\partial^2 \sigma}{\partial E \partial \Omega}(E, \mathbf{Q}) = \xi \sum_{I,F} \frac{k_F}{k_I} |\langle I k_I | V | k_F F \rangle|^2 \delta(E_I - E_F) \approx S(\mathbf{q}, \omega)$$

$V = 1/|r - r'|$  Coulomb interaction

Dynamic Structure Factor  $\sim$  Loss function

$$S(\mathbf{q}, \omega) \sim \text{Im } \epsilon^{-1}(\mathbf{q}, \omega)$$

Computational bottleneck:

Too many states!

All state  $k_F, k_I$  (probe) and  $F, I$  (sample) contribute

# Paradigm shift: Real-space Green's Function Approach

Golden rule *via* wavefunctions

$$\mu(E) \sim \sum_f |\langle i | \hat{\epsilon} \cdot \mathbf{r} | f \rangle|^2 \delta(E - E_f)$$

Golden rule via Green's functions:  $G = 1/(E - h - \Sigma)$

$$\mu(E) \sim -\frac{1}{\pi} \text{Im} \langle i | \hat{\epsilon} \cdot \mathbf{r}' G(\mathbf{r}', \mathbf{r}, E) \hat{\epsilon} \cdot \mathbf{r} | i \rangle$$

Efficient:

No sums over final states!



# Reviews of Modern Physics

JULY 2000

VOLUME 72 • NUMBER 3

PUBLISHED by THE AMERICAN PHYSICAL SOCIETY

through the AMERICAN INSTITUTE OF PHYSICS



THEORETICAL APPROACHES TO X-RAY  
ABSORPTION FINE STRUCTURE

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Use Prohibited Until 2005

# XAS & EELS

## Real-space Green's function theory

J. J. Rehr & R.C. Albers,  
Rev. Mod. Phys. **72**, 621 (2000)

<http://feffproject.org/feff/desy>

**Real-space multiple-scattering calculation and interpretation  
of x-ray-absorption near-edge structure**

A. L. Ankudinov

*MST-11, Los Alamos National Laboratory, Los Alamos, New Mexico 87545*

B. Ravel

*Ceramics Division, National Institute of Standards and Technology, Gaithersburg, Maryland 20899*

J. J. Rehr

*Department of Physics, University of Washington, Seattle, Washington 98195-1560*

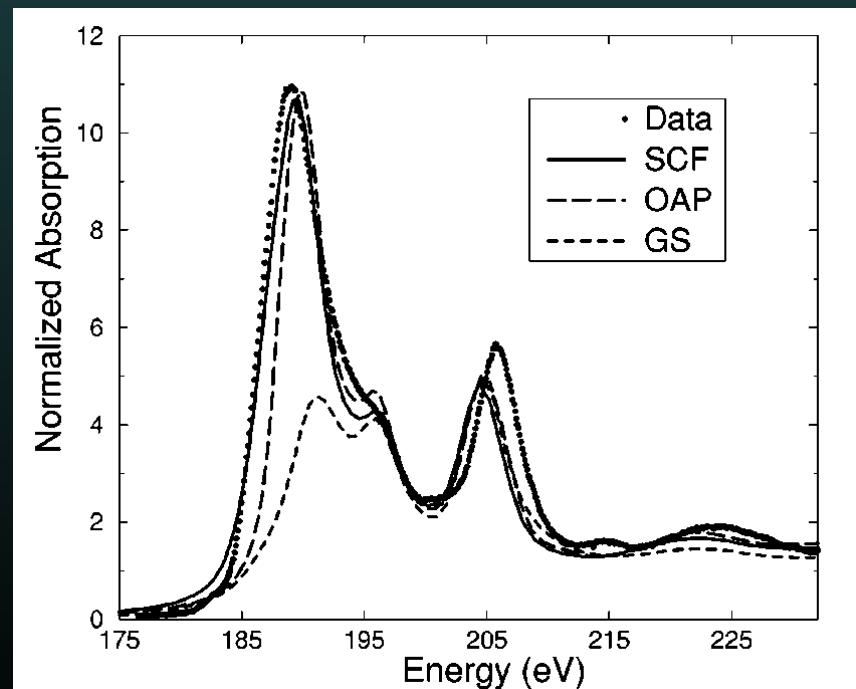
S. D. Conradson

*MST-11, Los Alamos National Laboratory, Los Alamos, New Mexico 87545*

**FEFF8**

Core-hole  
SCF potentials  
Self-energy  
DW factors

Efficient Core level spectra:  
EELS, XAS, XES



89 atom BN cluster

# Parallel (MPI) FEFF

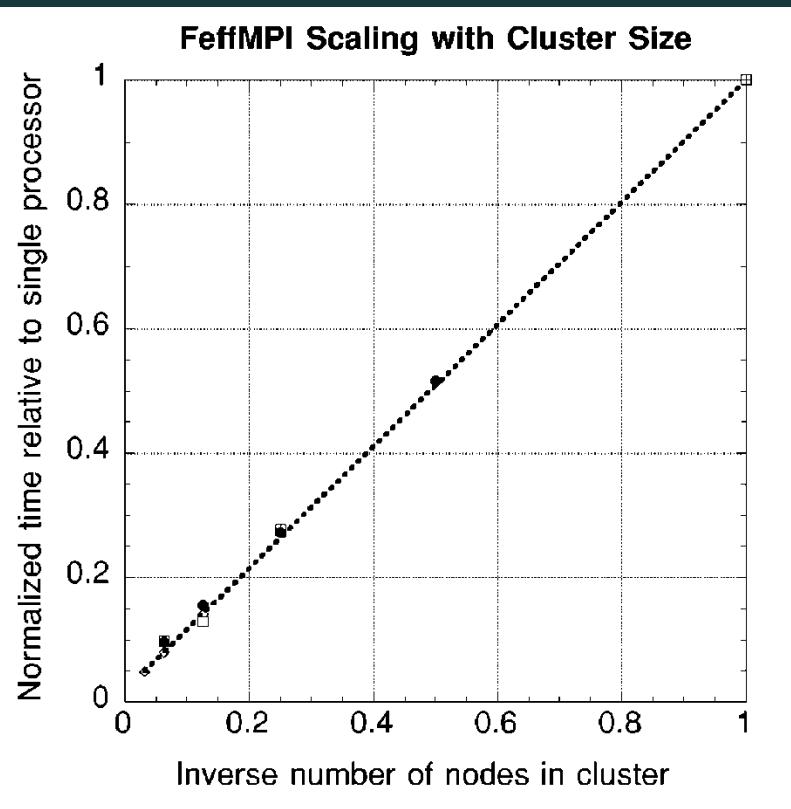
PHYSICAL REVIEW B, VOLUME 65, 104107

## Parallel calculation of electron multiple scattering using Lanczos algorithms

A. L. Ankudinov,<sup>1</sup> C. E. Bouldin,<sup>2</sup> J. J. Rehr,<sup>1</sup> J. Sims,<sup>2</sup> and H. Hung<sup>2</sup>

<sup>1</sup>*Department of Physics, University of Washington, Seattle, Washington 98195*

<sup>2</sup>*National Institute of Standards and Technology, Gaithersburg, Maryland 20899*



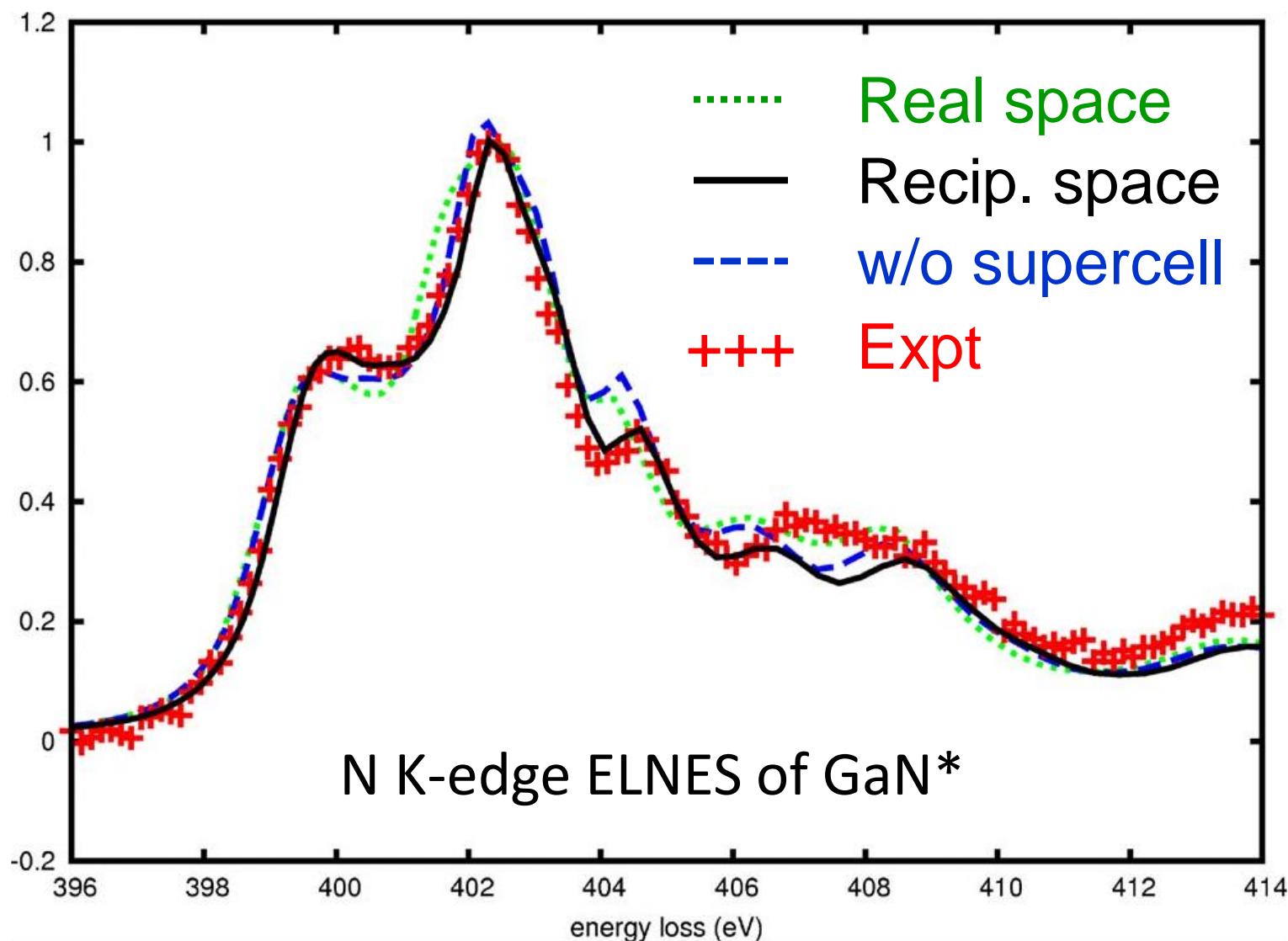
$$\mu(\mathbf{E}) \sim -\frac{1}{\pi} \operatorname{Im} \langle i | \hat{\epsilon} \cdot \mathbf{r}' G(\mathbf{r}', \mathbf{r}, \mathbf{E}) \hat{\epsilon} \cdot \mathbf{r} | i \rangle$$

MPI: “Natural parallelization”  
Each proc. does a  
few **energies**

Needed for state-of-the-art  
XANES simulations

# EELS in FEFF9: Impurity Green's function

## EELS in periodic systems w/o supercell\*



\*K. Jorissen & J. J. Rehr Phys. Rev. B 81, 245124 (2010)

# Relativistic corrections to EELS\*

## Relativistic Coulomb interaction

$$\frac{\partial^2 \sigma}{\partial E \partial \Omega}(E, \mathbf{Q}) = \xi \frac{k'}{k} \frac{1}{(Q^2 - E/\hbar c)^2} \sum_{I,F} |\langle I | \mathbf{r} \cdot \mathbf{Q}' | F \rangle|^2 \delta(E_I - E_F - E)$$

$$\frac{\partial^2 \sigma}{\partial E \partial \Omega}(E, \mathbf{Q}) = f(Q) \sum_{i,j=1}^3 Q'_i Q'_j \sigma_{ij}(E)$$

where

$$\mathbf{Q}' = \mathbf{Q} - Q_z \beta^2 \mathbf{e}_z$$

and the abs.  
tensor is

$$\sigma_{ij}(E) = \xi' E \sum_{I,F} \langle F | r_i | I \rangle \langle I | r_j | F \rangle \delta(E_I - E_F - E)$$

# Relativistic EELS

PHYSICAL REVIEW B 81, 155108 (2010)

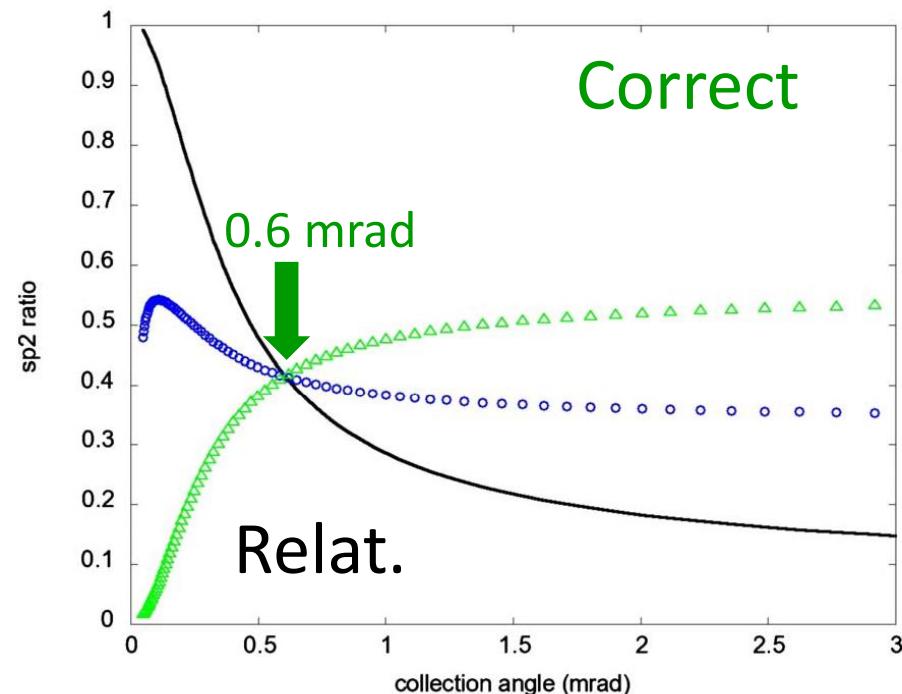
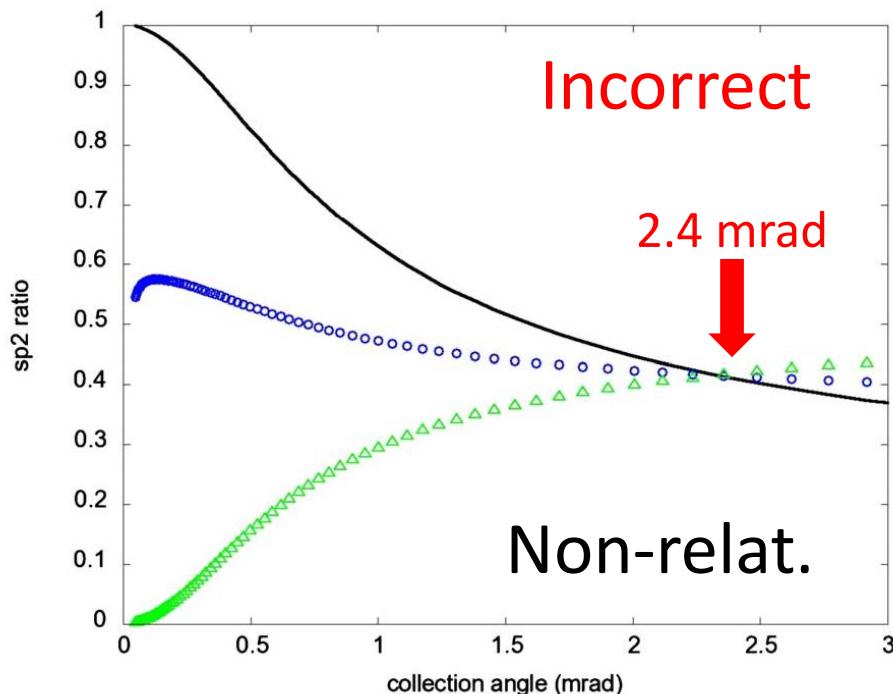
## Multiple scattering calculations of relativistic electron energy loss spectra

K. Jorissen,<sup>1</sup> J. J. Rehr,<sup>1,\*</sup> and J. Verbeeck<sup>2</sup>

<sup>1</sup>*Department of Physics, University of Washington, Seattle, Washington 98195, USA*

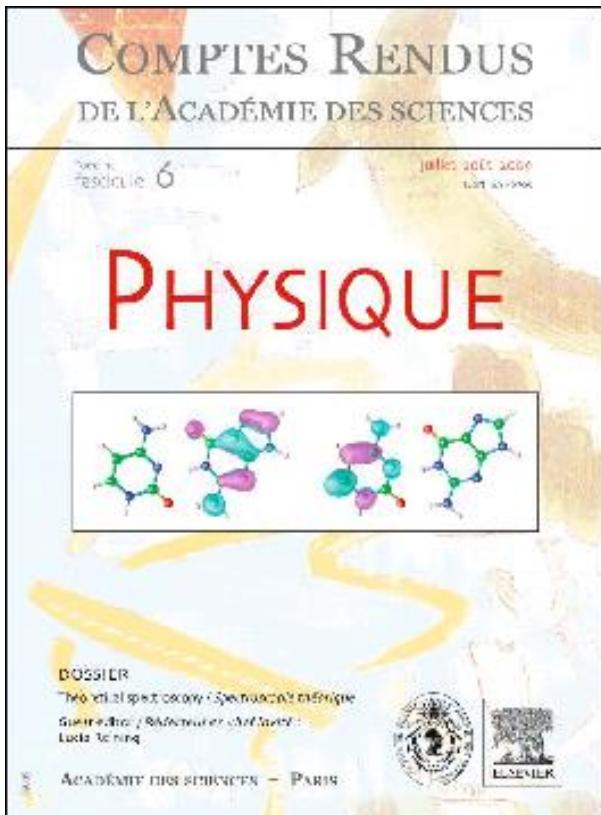
<sup>2</sup>*EMAT, University of Antwerp, Groenenborgerlaan 171, B2020, Antwerp, Belgium*

(Received 26 October 2009; revised manuscript received 30 March 2010; published 13 April 2010)



Relativistic Magic Angle in FEFF9 agrees with expt.

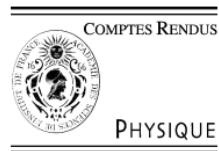
# FEFF9: Advanced methods



Available online at [www.sciencedirect.com](http://www.sciencedirect.com)



C. R. Physique 10 (2009) 548–559

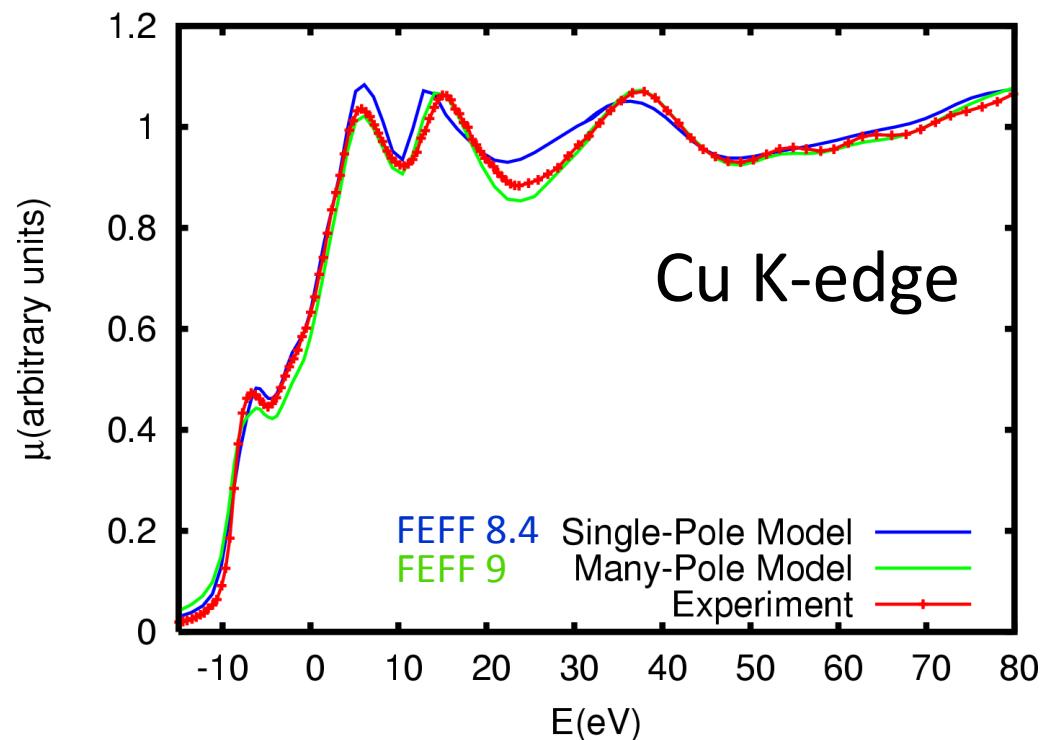


<http://france.elsevier.com/direct/COMREN/>

Theoretical spectroscopy / Spectroscopie théorique

*Ab initio* theory and calculations of X-ray spectra

John J. Rehr \*, Joshua J. Kas, Micah P. Prange, Adam P. Sorini, Yoshinari Takimoto,  
Fernando Vila



# FEFF9: Advanced methods

PERSPECTIVE

[www.rsc.org/pccp](http://www.rsc.org/pccp) | Physical Chemistry Chemical Physics

## Parameter-free calculations of X-ray spectra with FEFF9

John J. Rehr,<sup>\*a</sup> Joshua J. Kas,<sup>a</sup> Fernando D. Vila,<sup>a</sup> Micah P. Prange<sup>bc</sup> and Kevin Jorissen<sup>a</sup>

Received 15th December 2009, Accepted 27th April 2010

First published as an Advance Article on the web 6th May 2010

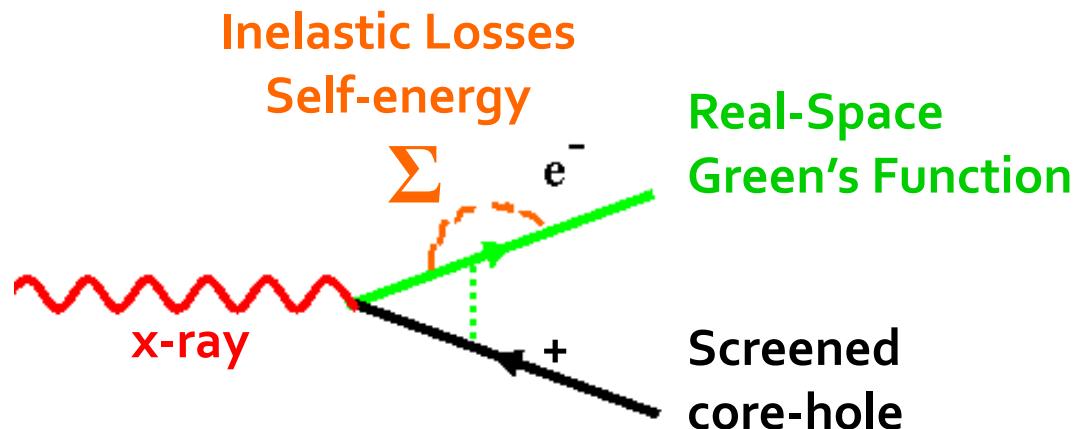
DOI: 10.1039/b926434e

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*Phys. Chem. Chem. Phys.*, 2010, 12, 5503–5513 | 5503

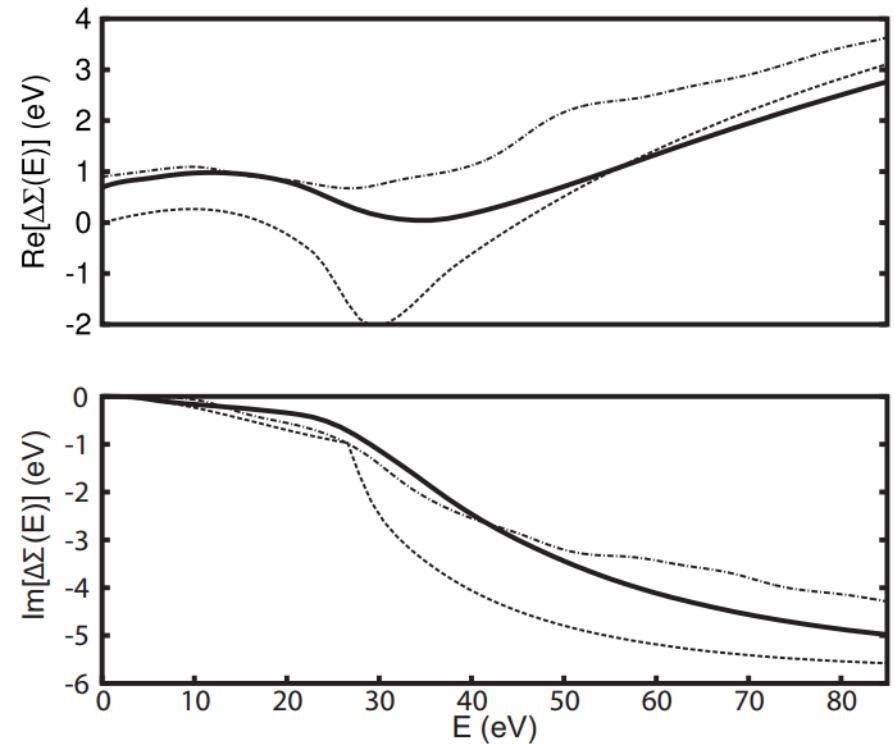
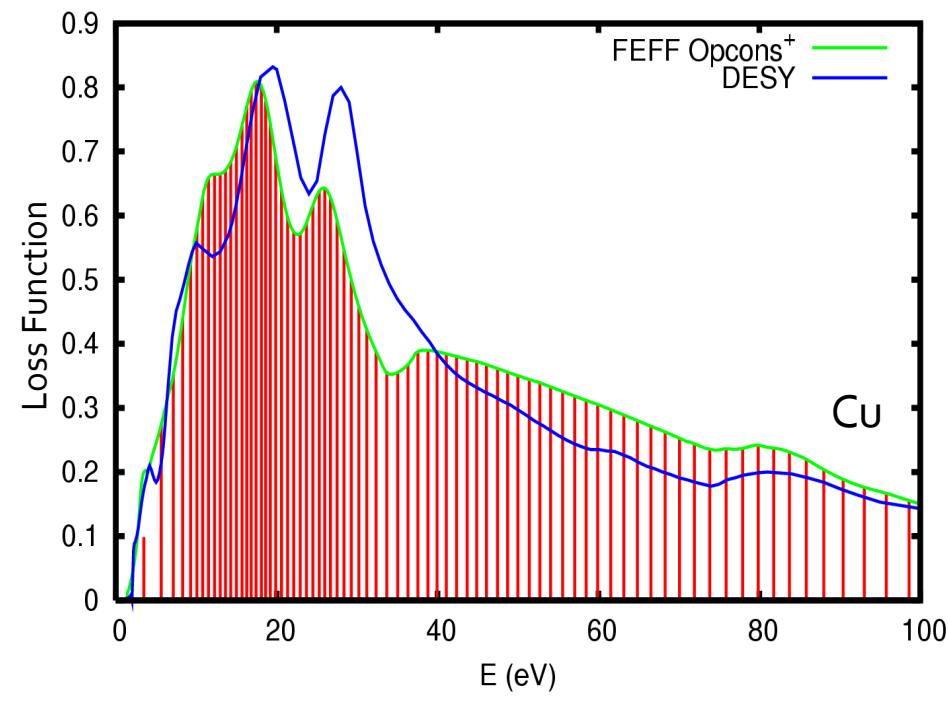
Ab initio:

Mean free paths  
Self-energies  
Debye-Waller factors  
RPA core-hole screening  
Multi-electron excitations



# Many-Pole Self-Energy (MPSE)

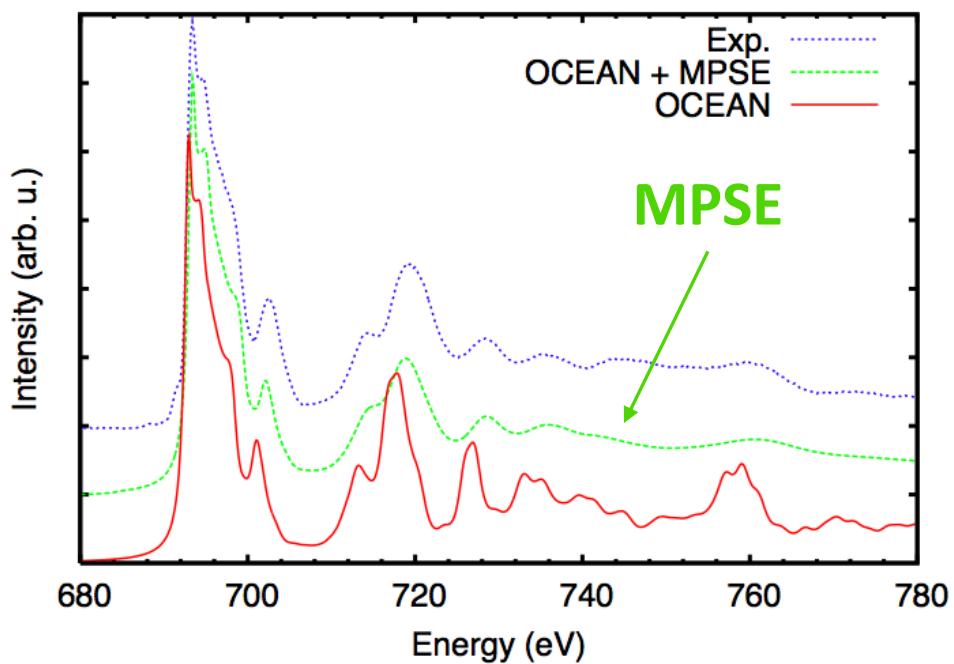
Extension of Hedin-Lundqvist (HL) plasmon-pole (pp) GW SE model  
 $\Sigma$  approximated as sum of PP models matched to loss function



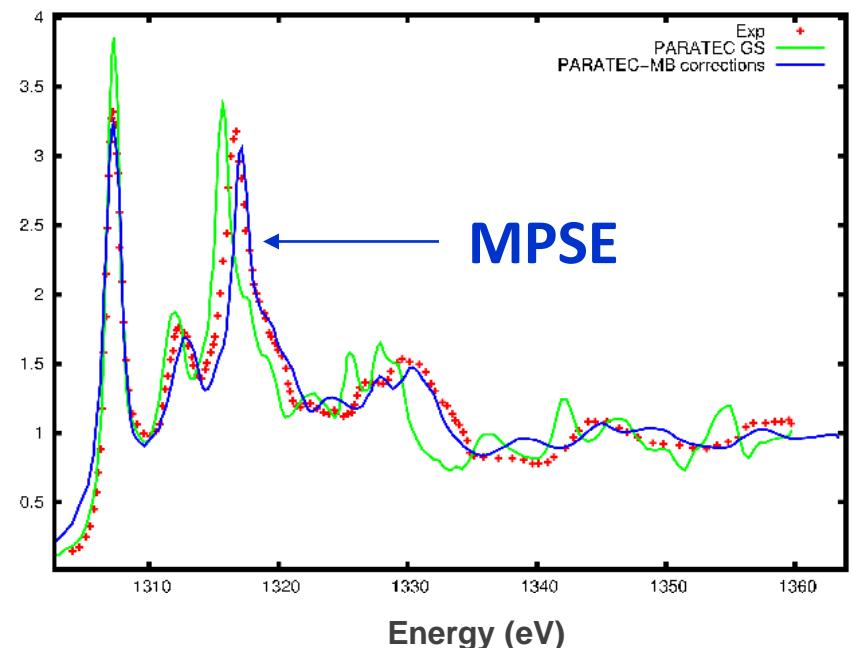
Many-pole (full) much better than HL (dashed) vs better theory (dot-dashed)

# MPSE corrections in BSE and DFT\*

LiF (BSE+MPSE)

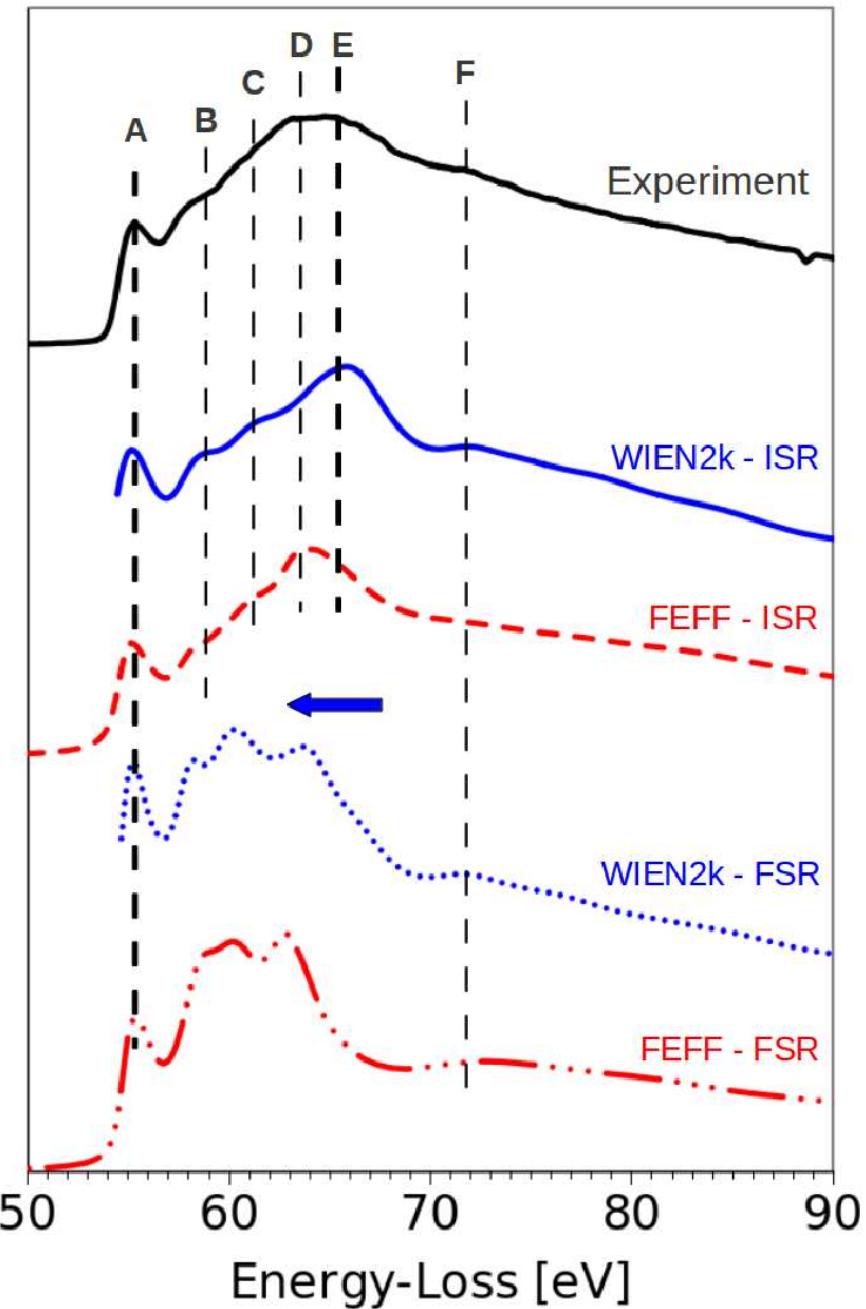


$\text{MgAl}_2\text{O}_4$  ( $\Delta\text{SCF}$ -DFT+MPSE)



# Question: Can we improve the theory?

V. Mauchamp, M. Jaouen, JJR, and J. J.  
Kas, U. Poitiers, Preprint (2010)



# Answer: GW/BSE

# Ab initio optical & low-loss spectra

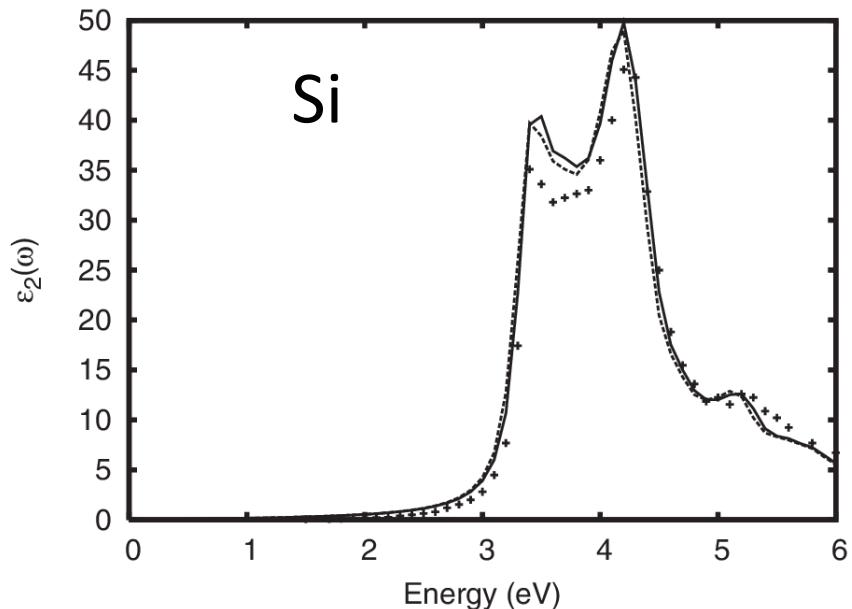
PHYSICAL REVIEW B 78, 205108 (2008)

## Optical to UV spectra and birefringence of $\text{SiO}_2$ and $\text{TiO}_2$ : First-principles calculations with excitonic effects

H. M. Lawler,<sup>1</sup> J. J. Rehr,<sup>1</sup> F. Vila,<sup>1</sup> S. D. Dalosto,<sup>1,2</sup> E. L. Shirley,<sup>2</sup> and Z. H. Levine<sup>2</sup>

<sup>1</sup>*Department of Physics, University of Washington, Seattle, Washington 98195, USA*

<sup>2</sup>*National Institute of Standards and Technology, Gaithersburg, Maryland 20899, USA*



AI2NBSE:  
Abinit+NIST BSE+UW MPSE

Plane-wave, pseudo-potential  
GW/BSE code

UW + NIST collaboration

# Ab initio GW/BSE core-spectra: ELNES & XANES

PHYSICAL REVIEW B 83, 115106 (2011)

## Bethe-Salpeter equation calculations of core excitation spectra

J. Vinson, J. J. Rehr, and J. J. Kas

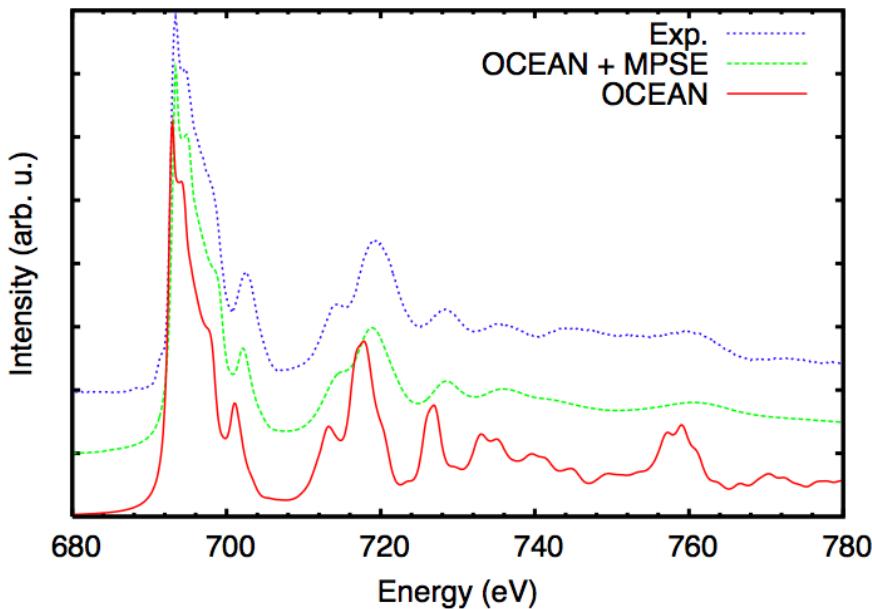
Department of Physics, University of Washington, Seattle, Washington 98195, USA

E. L. Shirley

National Institute of Standards and Technology (NIST), Gaithersburg, Maryland 20899, USA

(Received 29 September 2010; published 4 March 2011)

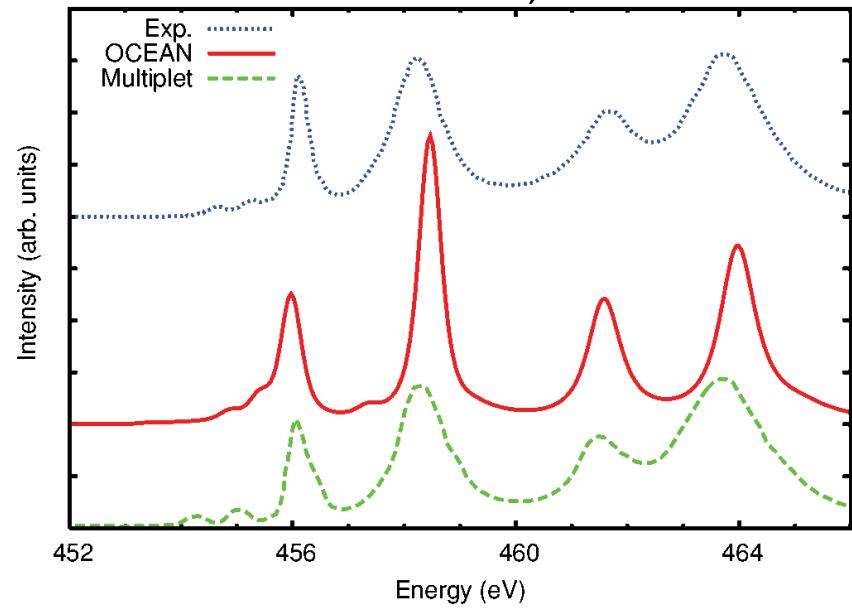
## LiF: F K edge



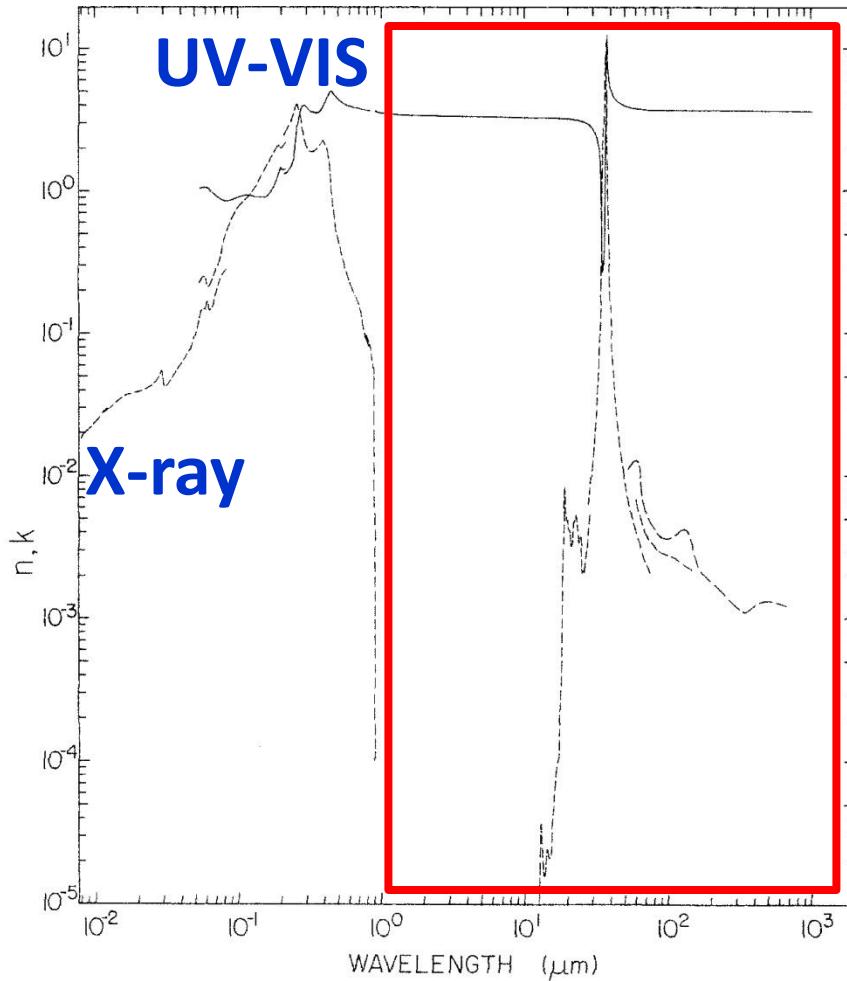
OCEAN: Obtaining Core  
Excitations from  
Abinit and NBSE

UW + NIST Collaboration

## SrTiO<sub>3</sub>: Ti L<sub>2,3</sub> edge



# Are we there yet? Optical constants: THz to X-ray



Challenge:  
Efficient phonon  
spectra

Can we compute  
vibrational properties ab  
initio?

# Ab initio Debye Waller Factors: $e^{-2\sigma_R^2 k^2}$

Projected Vibrational DOS: Use efficient pole model

$$\rho_R(\omega) = -\frac{2\omega}{\pi} \text{Im} \left\langle 0 \left| \frac{1}{\omega^2 - \mathbf{D} + i\varepsilon} \right| 0 \right\rangle \cong \sum_{v=1}^N w_v \delta(\omega - \omega_v)$$



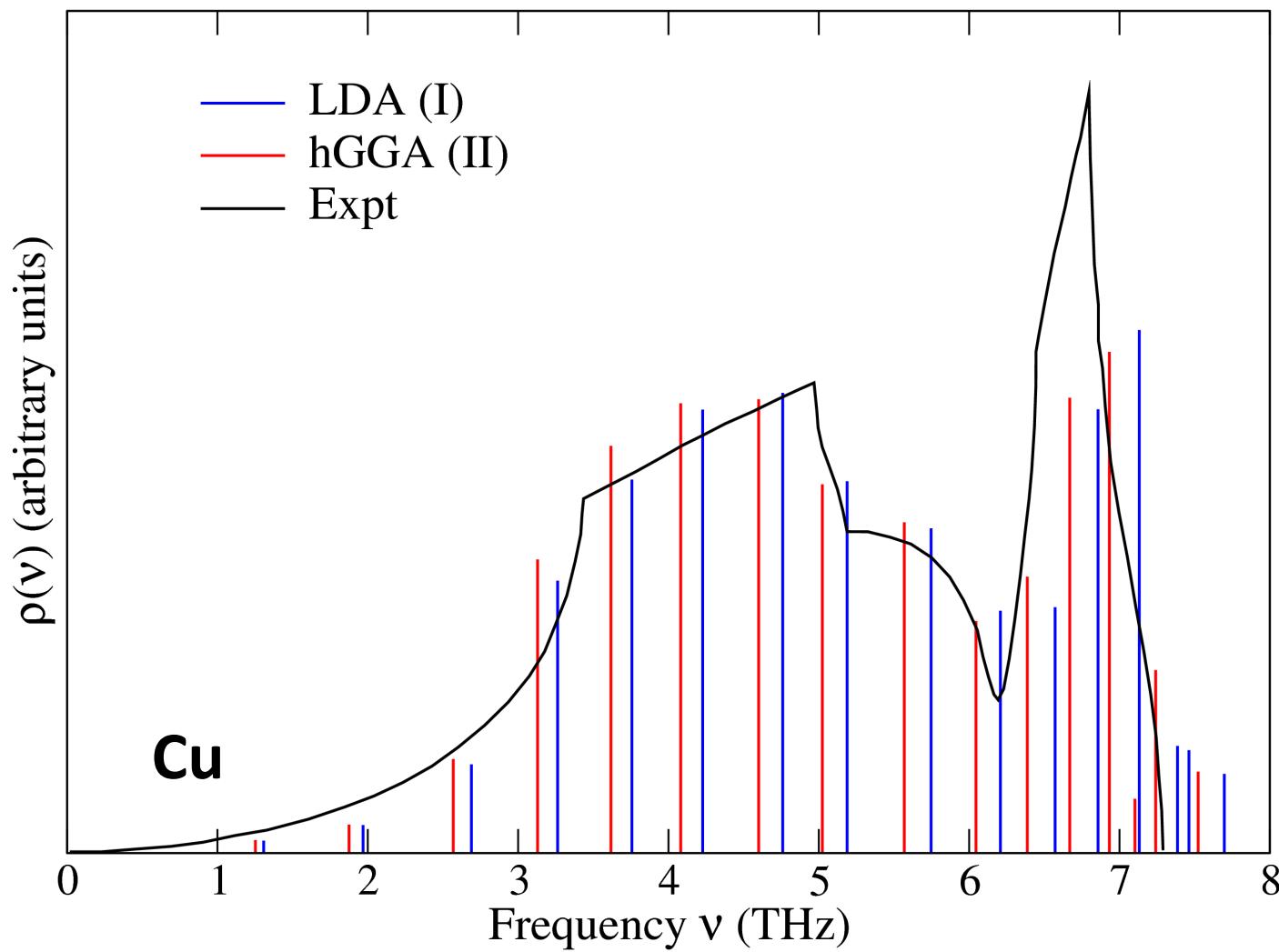
EXAFS MSRDs:

$$\sigma_R^2(T) = \frac{\hbar}{2\mu_R} \int_0^\infty \frac{1}{\omega} \coth\left(\frac{\beta\hbar\omega}{2}\right) \rho_R(\omega) d\omega$$

Helmholtz  
Free Energy:

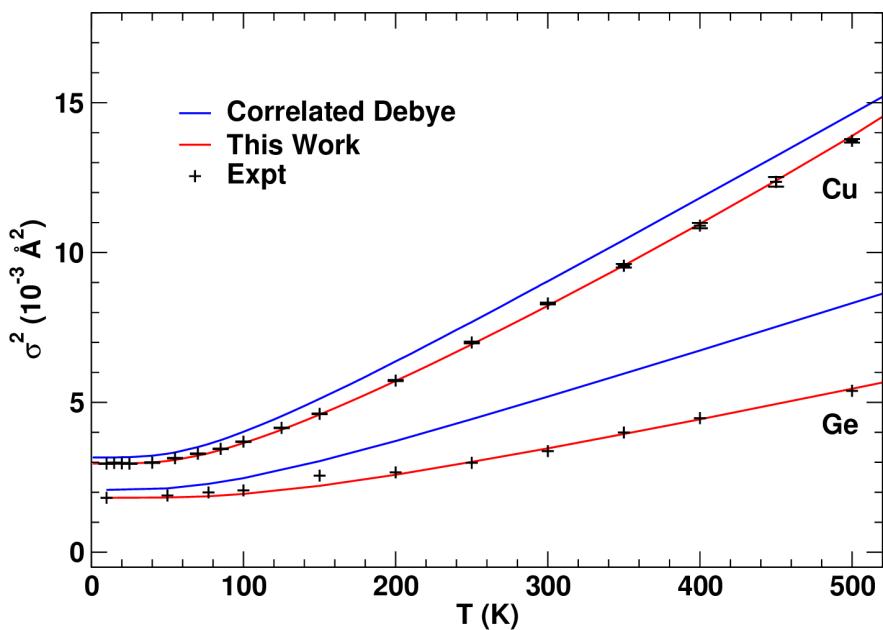
$$F(T) = E + k_B T \sum_i^{N_{coor}} \int_0^\infty \ln \left[ 2 \sinh \left( \frac{\beta\hbar\omega}{2} \right) \right] \rho_i(\omega) d\omega$$

# Vibrational Density of States

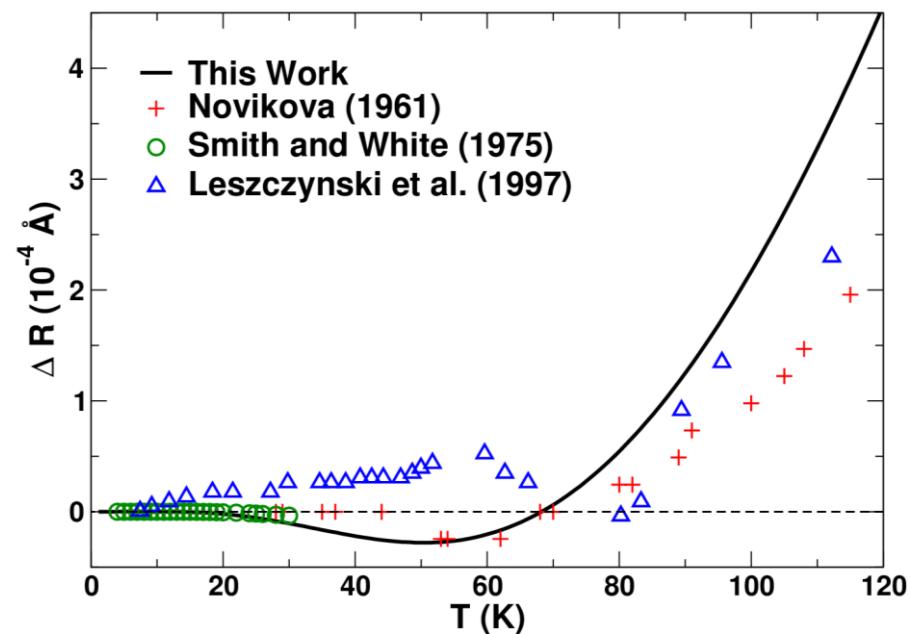


# Typical Results

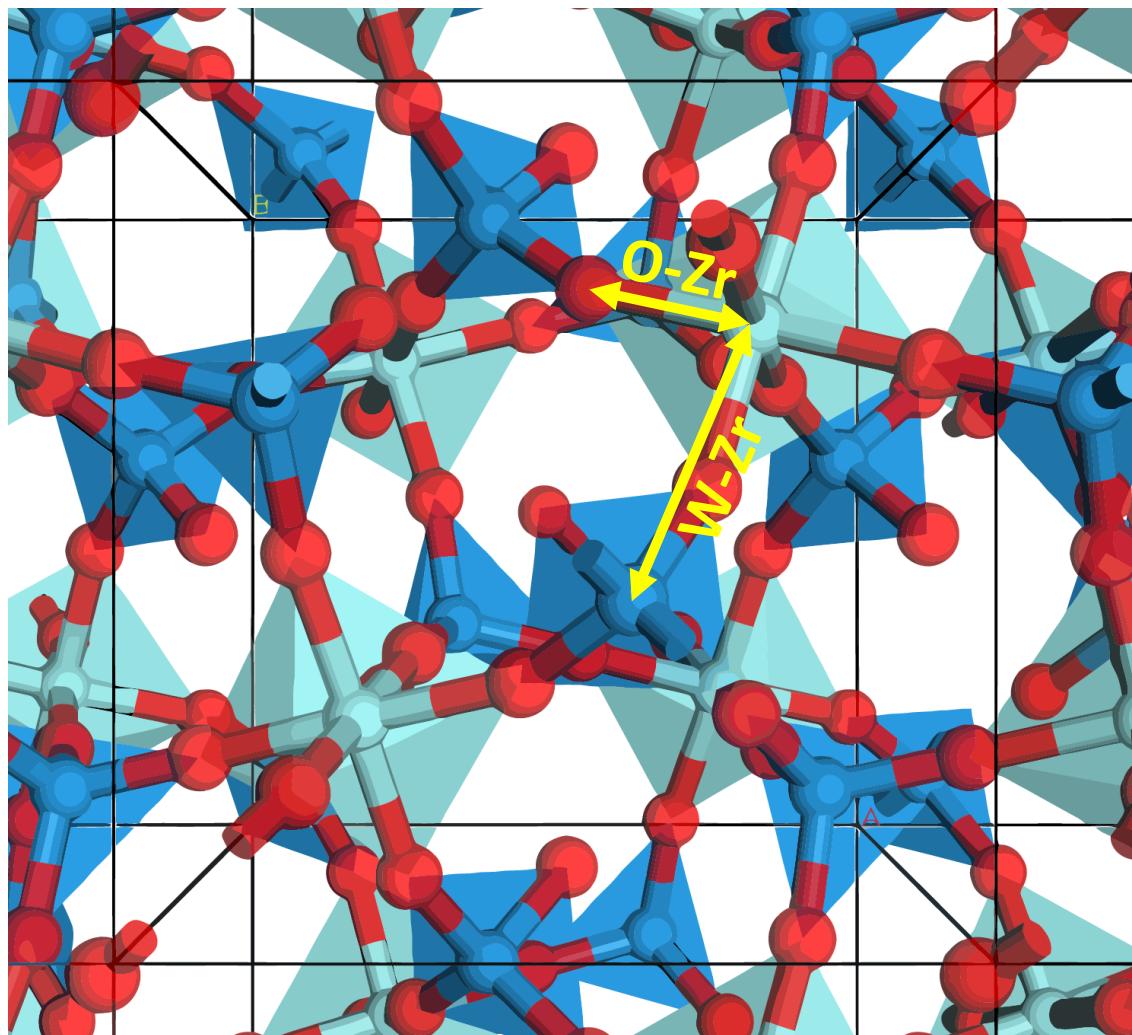
Cu and Ge: NN MSRD



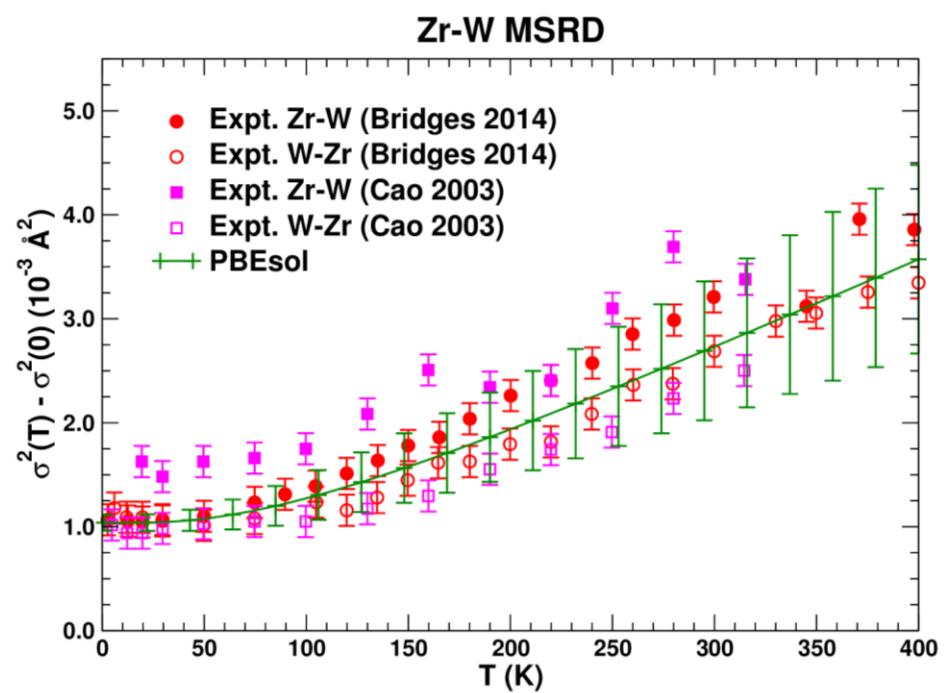
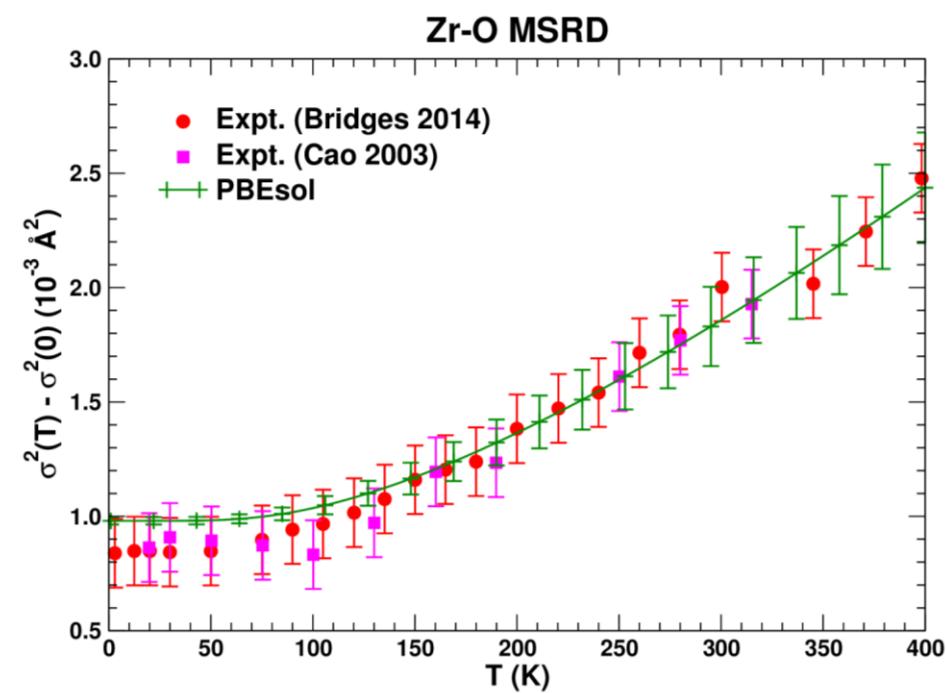
GaAs: Negative Thermal Expansion



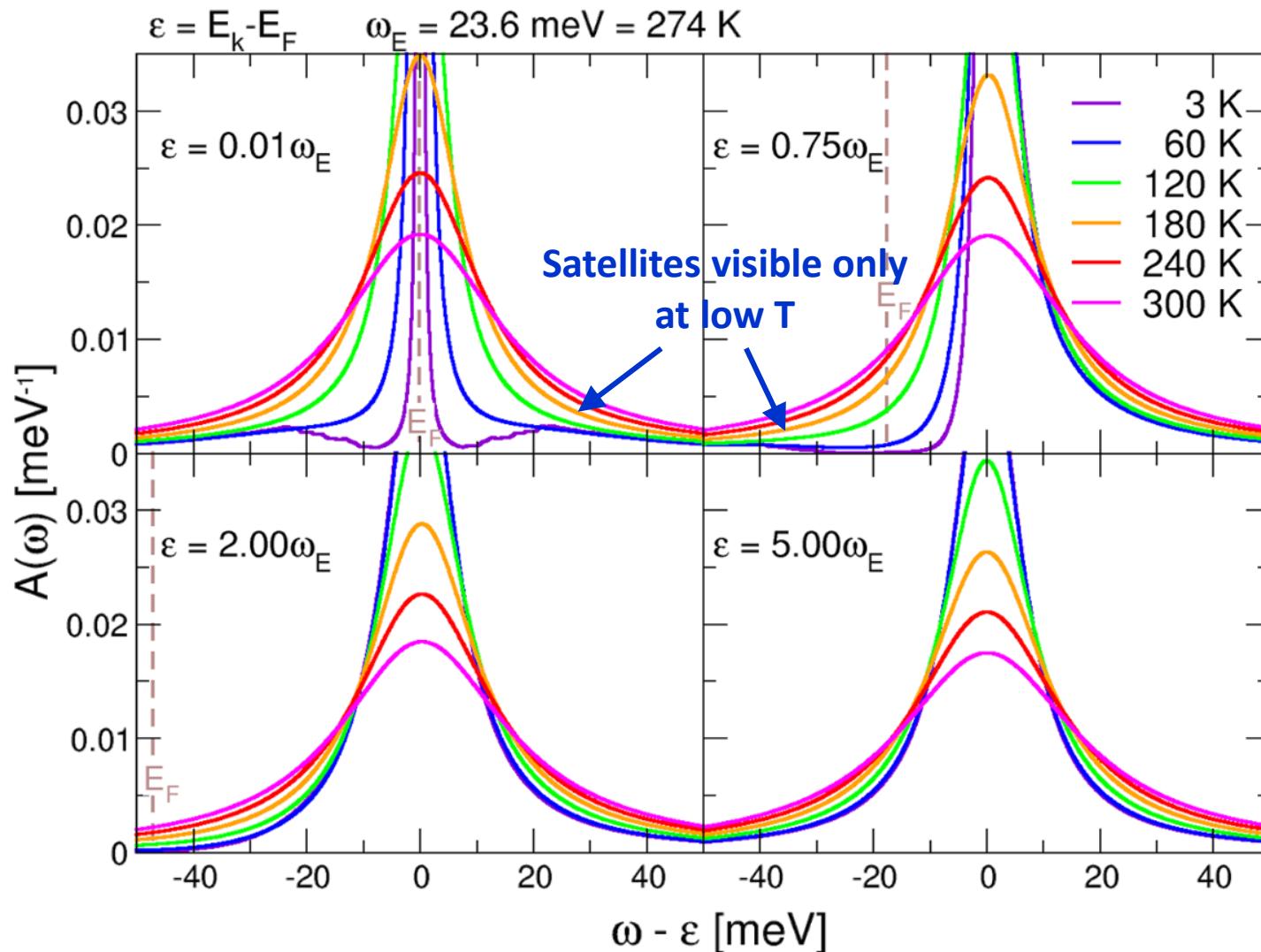
# ZrW<sub>2</sub>O<sub>8</sub>: Complex unit cell



# $\text{ZrW}_2\text{O}_8$ : MSRDs



# Phonon-contributions to final-state broadening in Cu



# User-friendly Java GUI: JFEFF

15th International Conference on X-ray Absorption Fine Structure (XAFS15)

IOP Publishing

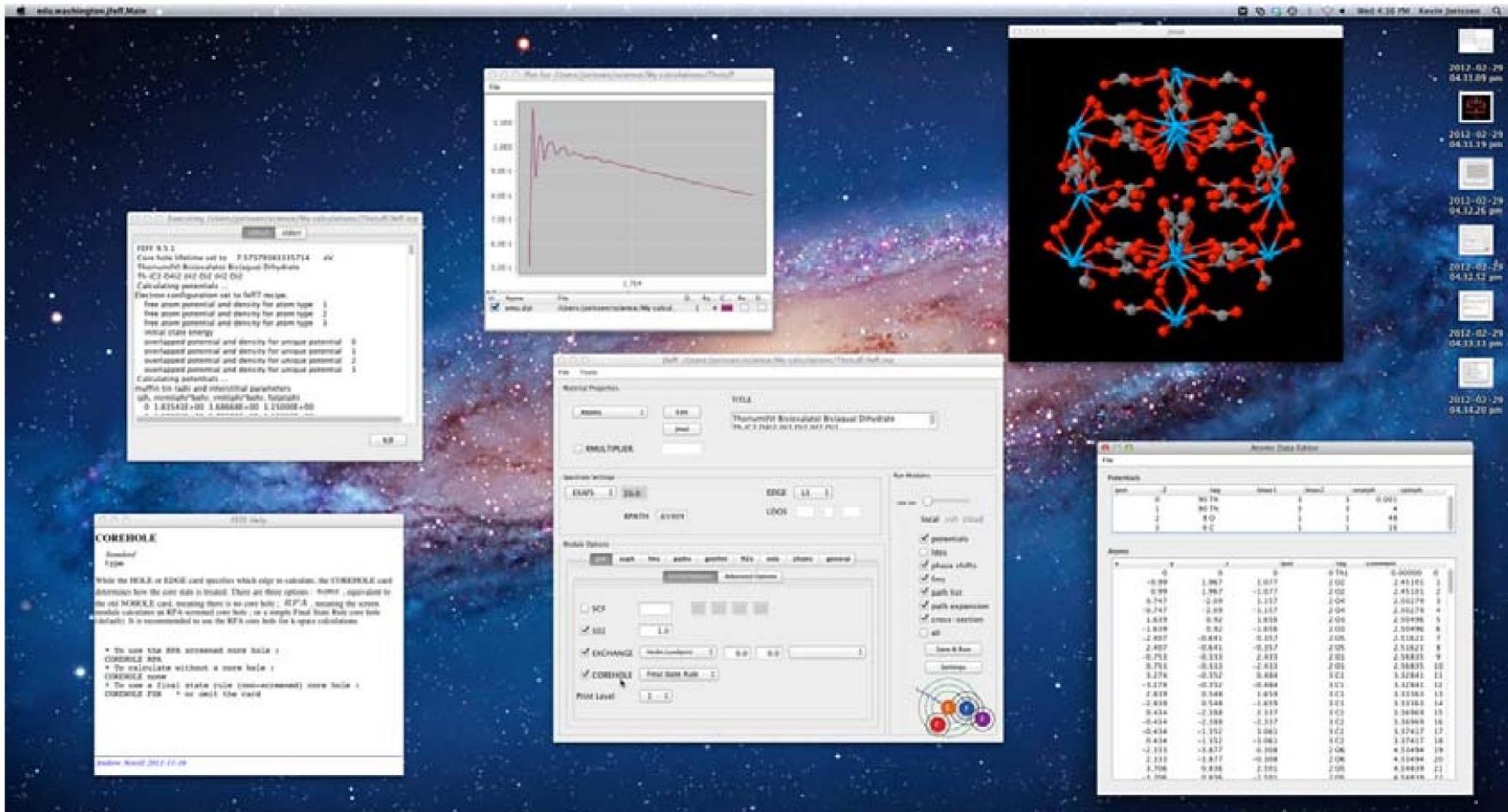
Journal of Physics: Conference Series 430 (2013) 012001

doi:10.1088/1742-6596/430/1/012001

# New Developments in FEFF: FEFF9 and JFEFF

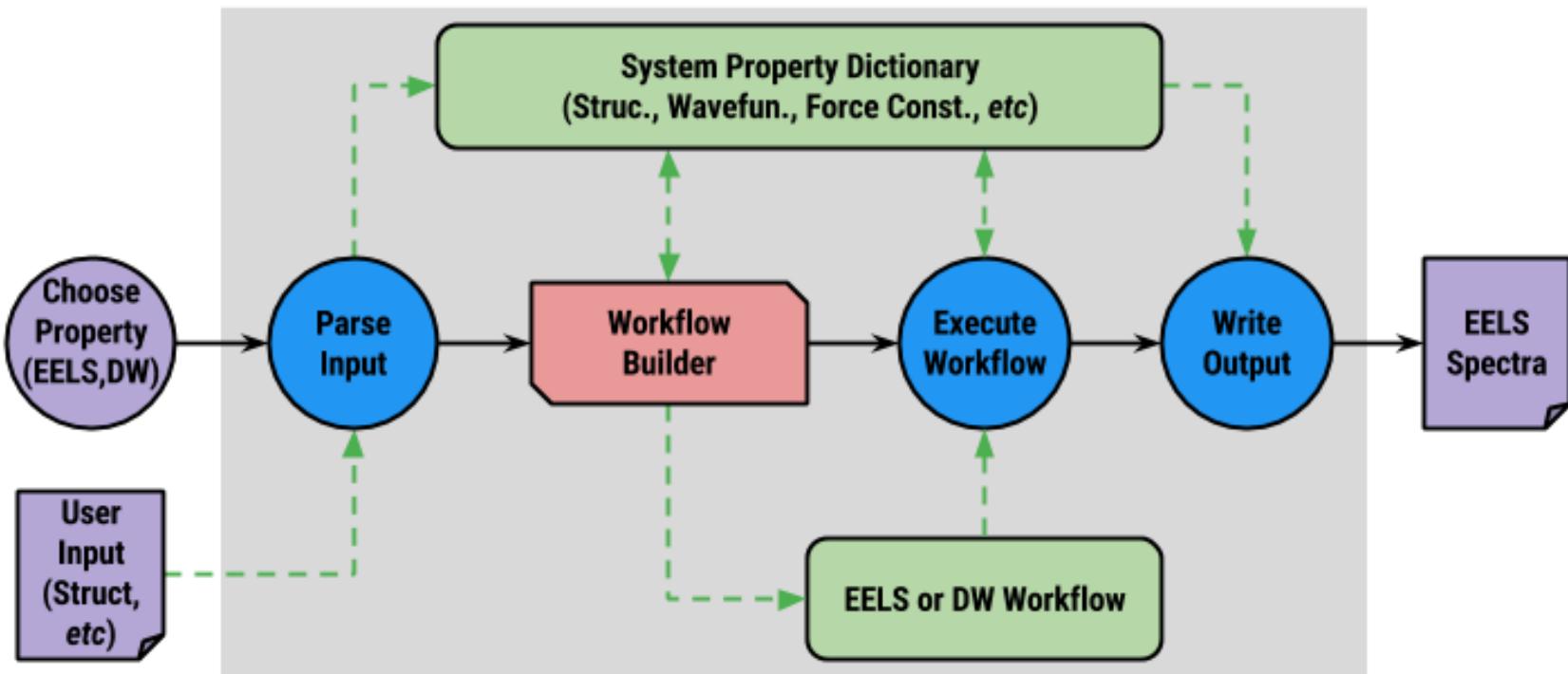
Kevin Jorissen and John J. Rehr

Department of Physics, University of Washington, Seattle, WA 98195, USA



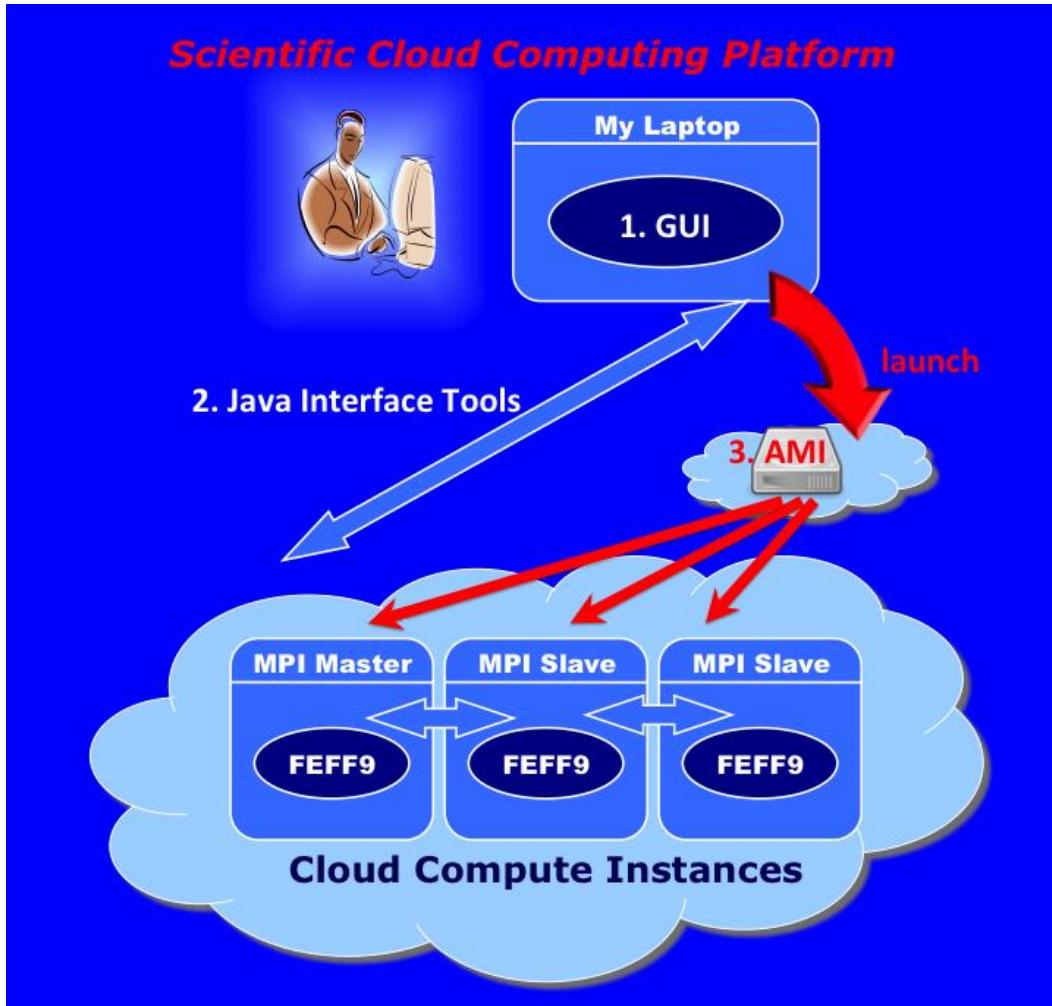
# VESPA - Virtual EELS Software Package

Goal: Integrated EELS software for STEM using CORVUS Workflow Manager



# Prototype: Virtual STEM in the Cloud

## State-of-the-art EELS modeling



FEFF9+JFEFF

AI2NBSE and OCEAN

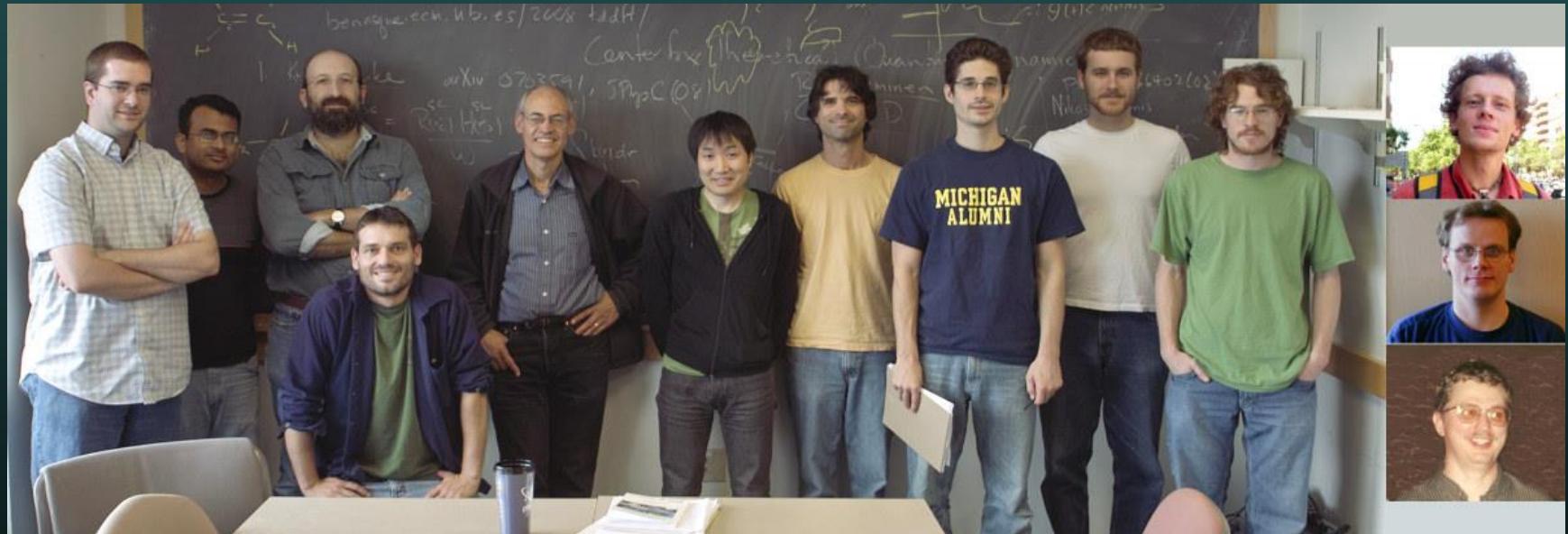
TELNES

Precompiled & Optimized  
on the Amazon EC2

# CONCLUSIONS

- Goals:
  - Mostly achieved or in sight
- Complementary theoretical techniques:
  - Real-space
  - Supercell/reciprocal space
- Next generation theory & codes including:
  - Many-body effects
  - Relativistic effects
- Broad spectrum response:
  - IR → VIS → UV → X-ray

# Acknowledgments: Thanks to DOE BES for \$\$ Rehr Group + L. Reining, M. Guzzo, E. Shirley, K. Gilmore, et al.



**From left to right:**

**Ken Nagle**

**Towfiq Ahmed**

**Fernando Vila**

**Micah Prange**

**John Rehr**

**Yoshi Takimoto**

**Hadley Lawler**

**Adam Sorini**

**John Vinson**

**Josh Kas**

**Kevin Jorissen**

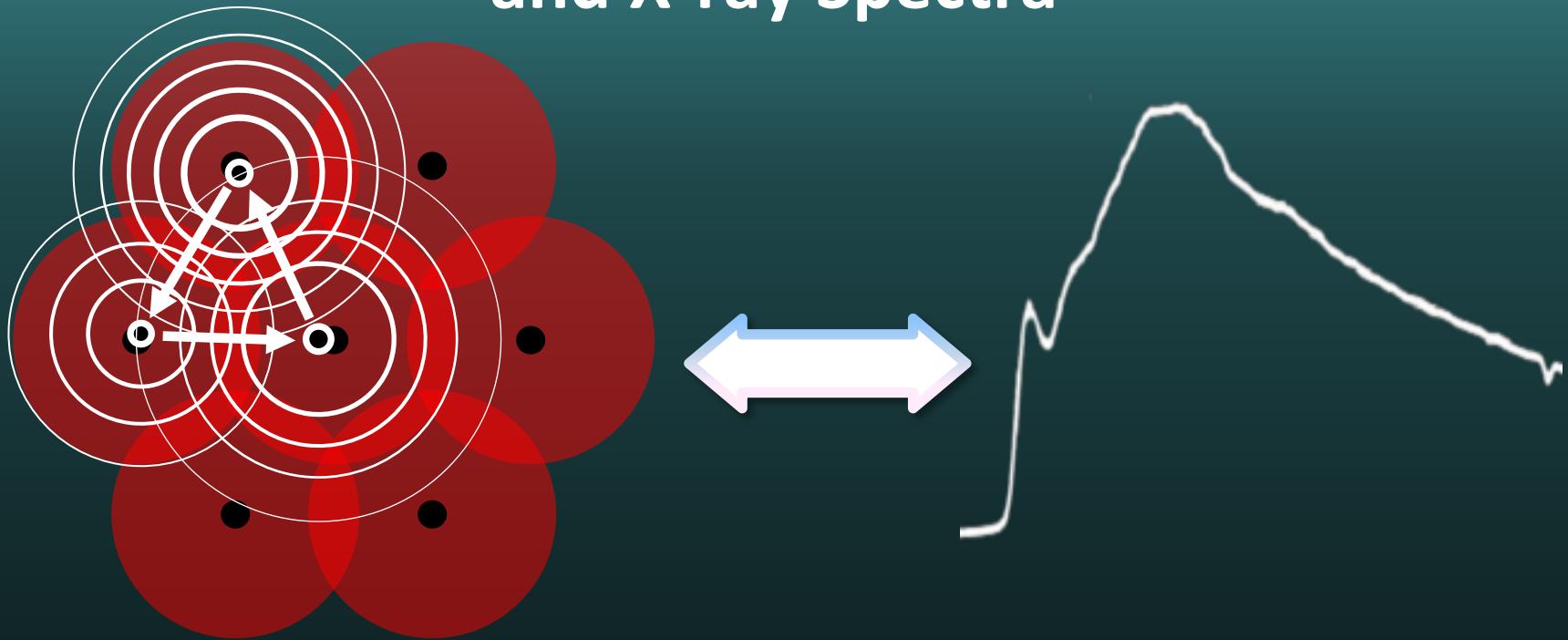
**Aleksi Soininen**

**Alex Ankudinov**

**(Shauna Story)**

**(Egor Clevac)**

# Theory and Parameter Free Calculations of EELS and X-ray Spectra



J.J. Rehr<sup>1</sup>, J. J. Kas<sup>1</sup>, K. Jorissen<sup>2</sup>, and F. Vila<sup>1</sup>

<sup>1</sup>Department of Physics, University of Washington, <sup>2</sup>Amazon Web Services  
Seattle, WA

Thank you!



