

# Molecular Properties of the Ice Ih Basal Surface

An Application of the SCME Water Interaction Potential



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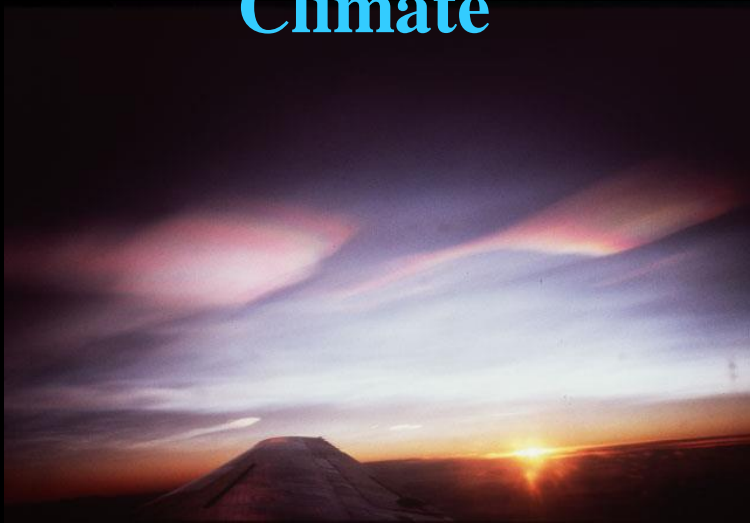
*University of Washington*

**Chemical  
Significance**

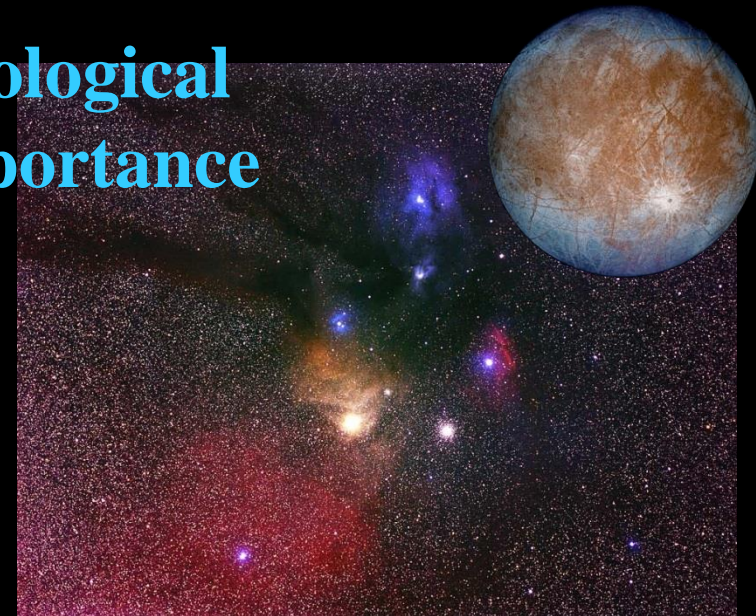


**Why  
Study Ice?**

**Environment,  
Weather and  
Climate**



**Biological  
Importance**



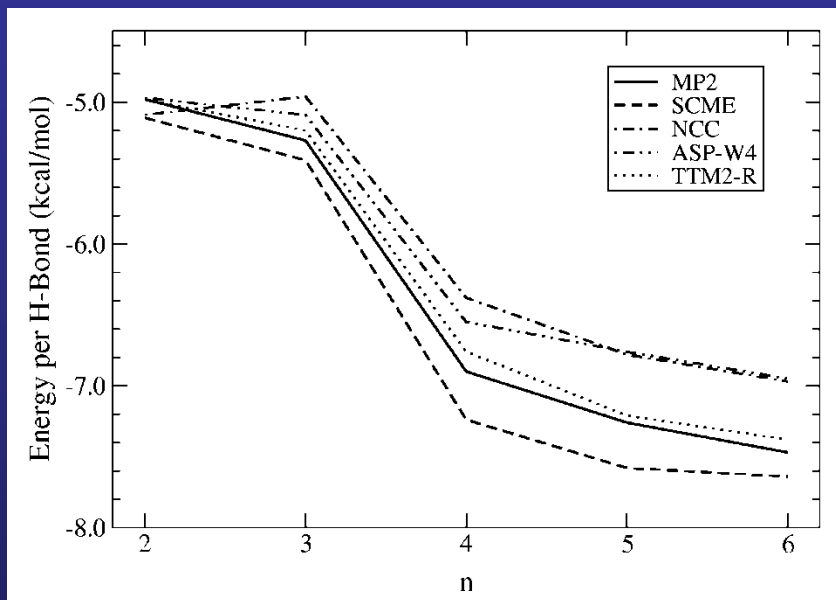
# The SCME Potential

- Based on a Single Center Multipole Expansion
- Does not use point charges
- Rigid
- Transferable
- Parametrized using a mixture of *ab initio* and empirical values

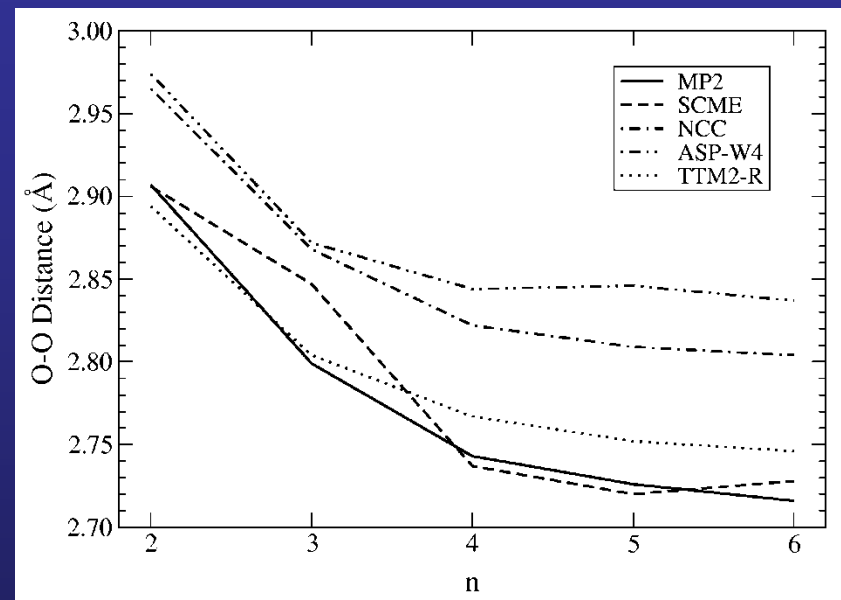
**Total Energy:**

$$E_{\text{tot}} = E_{\text{es+ind}} + E_{\text{disp}} + E_{\text{rep}}$$

# $(\text{H}_2\text{O})_{n=2-6}$ ring water clusters:

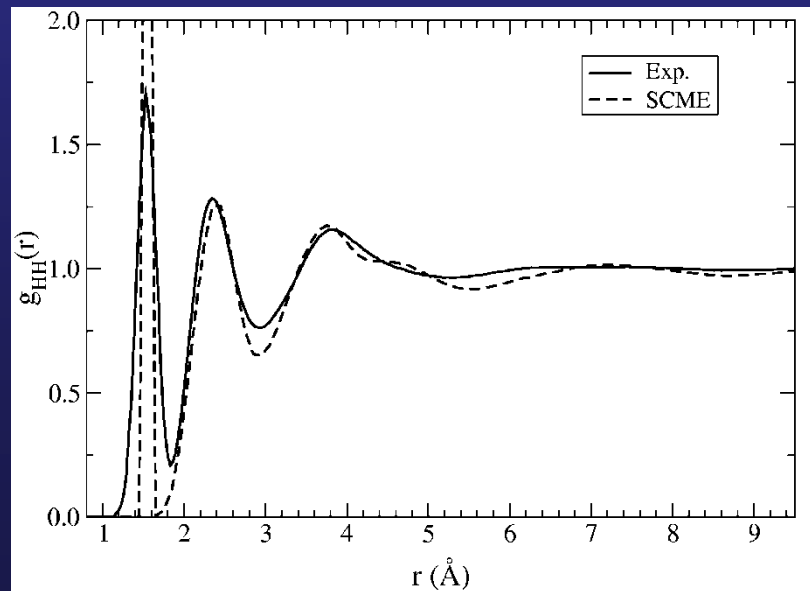
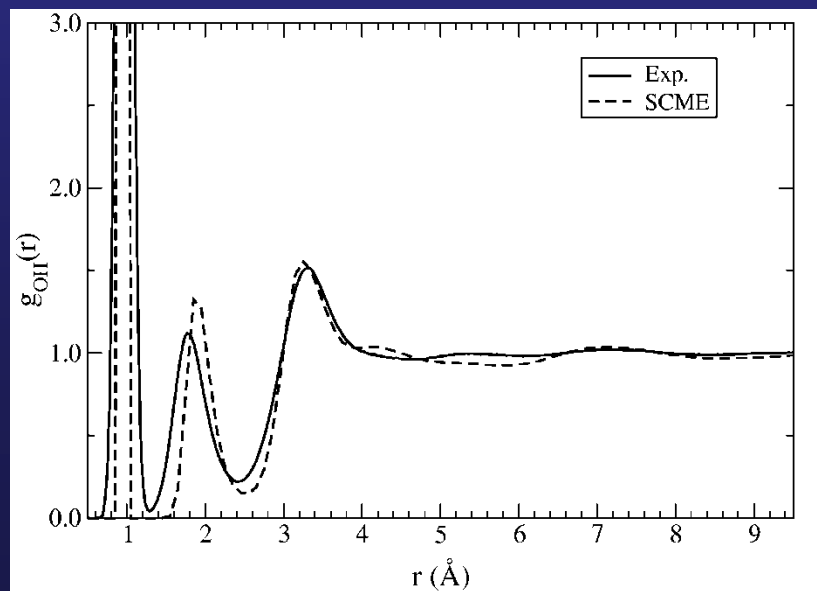
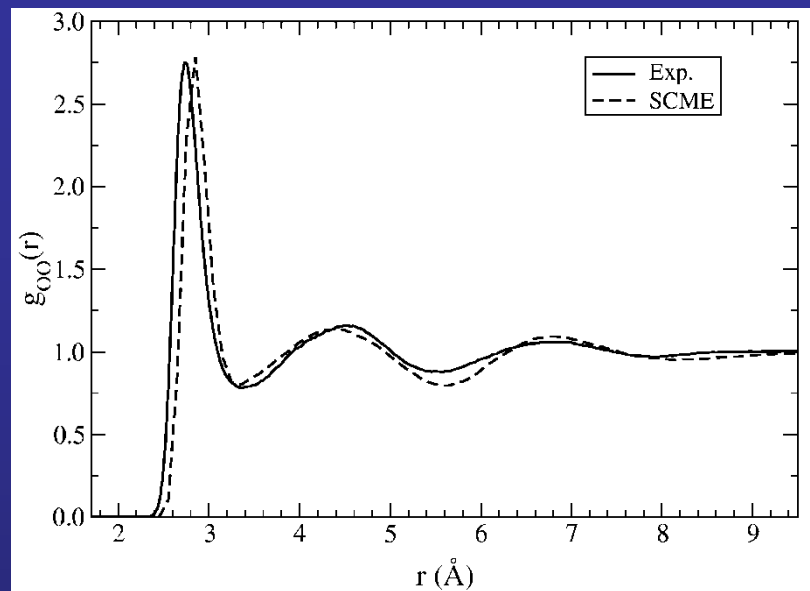


**Interaction Energy  
per H-Bond**



**Average O-O  
Distance**

# Radial Distribution Functions for Liquid Water:



# Bulk ice Ih:

Property	Exp. <sup>a</sup>	GGA	PW91 <sup>b</sup>	SCME	TIP4P	RWK2 <sup>c</sup>	DC	TTM2-R
Lattice Energy <sup>d</sup>	-0.6110		-0.55	-0.6109±0.0049	-0.634	-0.555	-0.550	-0.6370
$\langle r_{OO} \rangle^e$	2.751	2.70		2.742±0.004	2.683		2.738	
$a^e$	4.4969	4.41		4.470±0.025				4.478
$b^e$	7.7889	7.63		7.747±0.052				7.756
$c^e$	7.3211	7.20		7.287±0.029				7.314
$\rho^f$	0.933	0.989	0.954	0.948±0.004	1.009	0.942	0.960	0.942
$V_{molec}^g$	32.05	30.3	31.35	31.55±0.15	29.62	31.73	31.14	31.75
Bulk Modulus <sup>h</sup>	10.9		13.5	11.4±0.3	16.6	18.0		
$\mu_{molec}^i$	2.90		2.8	3.50±0.07	2.35		3.02	2.86 <sup>j</sup>

<sup>b</sup>All values taken from Ref.<sup>9</sup> except the bulk modulus, taken from Ref.<sup>78</sup>.

<sup>b</sup>From Ref.<sup>79</sup>

<sup>c</sup>From Ref.<sup>75</sup>

<sup>d</sup>In eV/molec

<sup>e</sup>In Å

<sup>f</sup>In Å<sup>3</sup>/molec

<sup>g</sup>In g/cm<sup>3</sup>

<sup>h</sup>In MPa

<sup>i</sup>In Debye

<sup>j</sup>Calculated at 100K

# Simulation of the Ice Ih Basal Surface

## General Properties of the Cells:

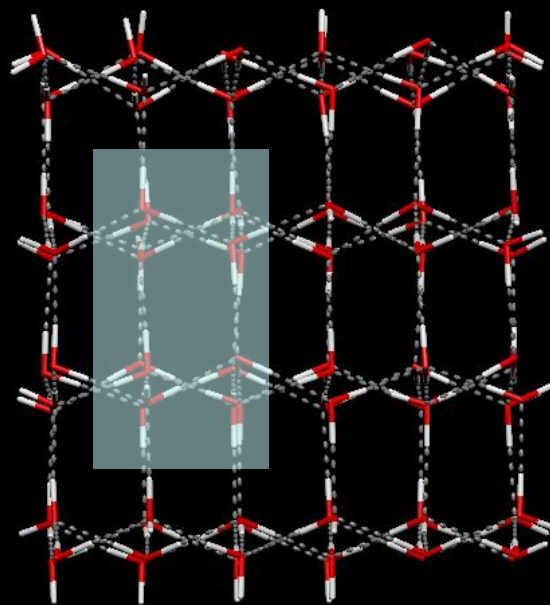
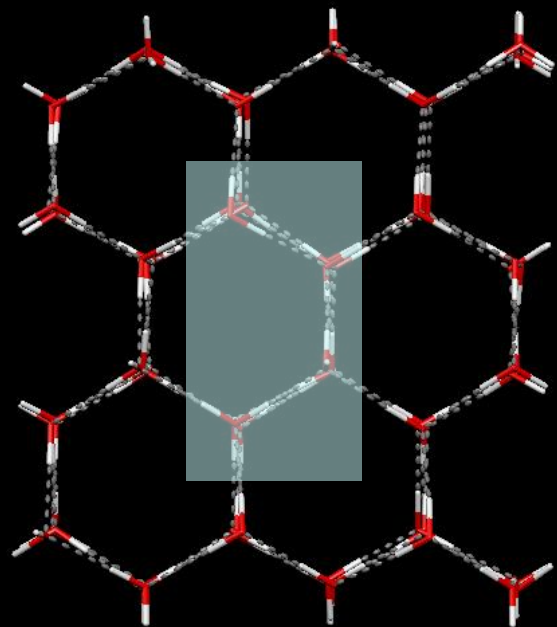
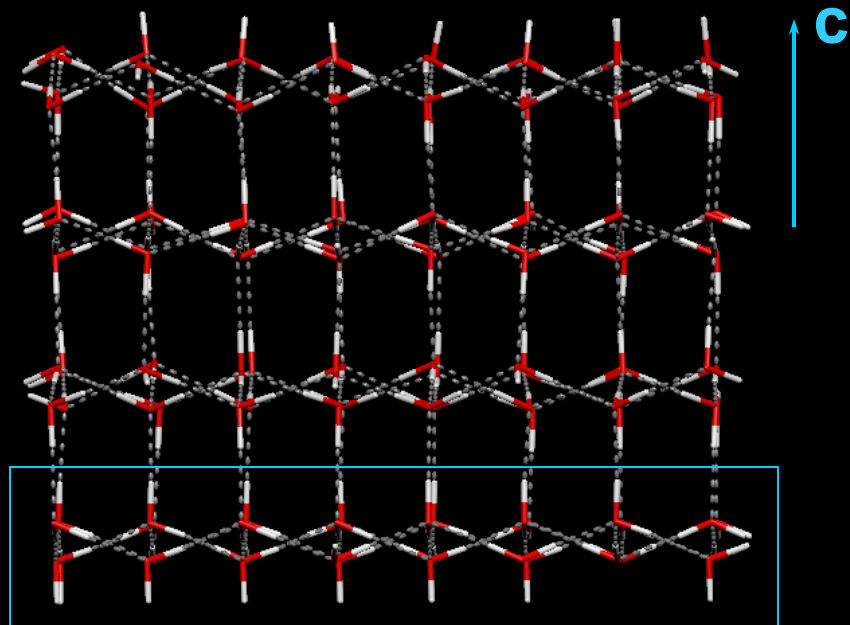
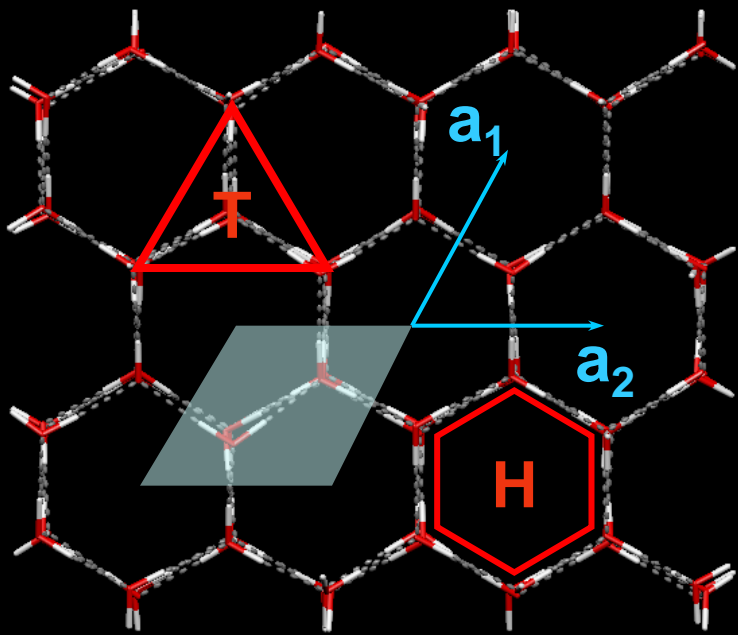
- Proton-disordered
- Null total dipole
- Four bilayers
- Bottom bilayer frozen at bulk conformation

## 5 Small Cells:

- 3 x 2 x 2 repetitions of the orthogonal cell
- 96 molecules per cell

## 10 Large Cells:

- 4 x 2 x 2 repetitions of the orthogonal cell
- 128 molecules per cell





# Binding energy (in eV) for the different types of minima:

	All			Large			Small		
	#	E	$\Delta E$	#	E	$\Delta E$	#	E	$\Delta E$
<b>DFAAH</b>	61	-0.612	0.097	40	-0.606	0.110	21	-0.623	0.074
<b>DDA-T</b>	52	-0.607	0.078	38	-0.611	0.081	14	-0.597	0.072
<b>DDA-H</b>	20	-0.590	0.070	13	-0.593	0.071	7	-0.586	0.068
<b>DFAAT</b>	24	-0.578	0.066	13	-0.570	0.071	11	-0.585	0.061
<b>DFA-I</b>	41	-0.539	0.074	33	-0.543	0.076	8	-0.525	0.066

One accepted Hydrogen-Bond

One “free” lone pair

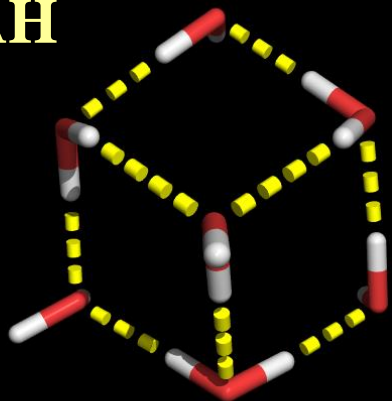
**DFA-H**

One donated hydrogen

One free Hydrogen

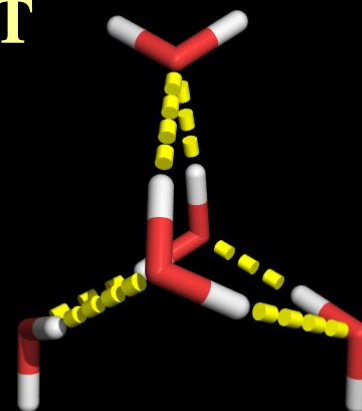
Over a hexagonal site

**DFAAH**



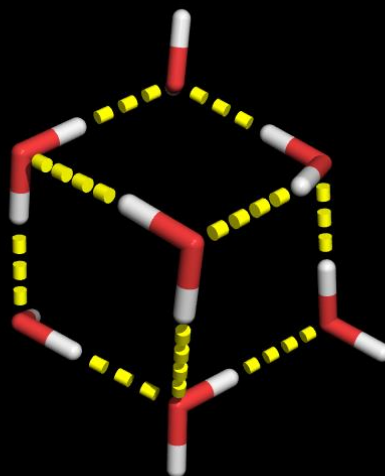
$$E_b = -0.612 \pm 0.097 \text{ eV}$$

**DDA-T**



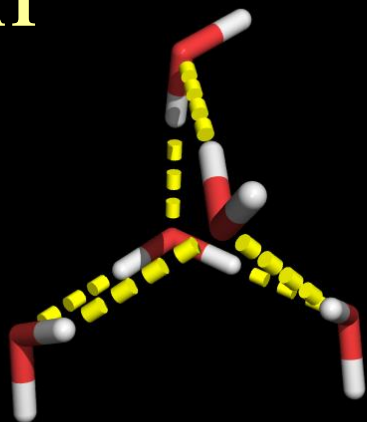
$$E_b = -0.607 \pm 0.078 \text{ eV}$$

**DDA-H**



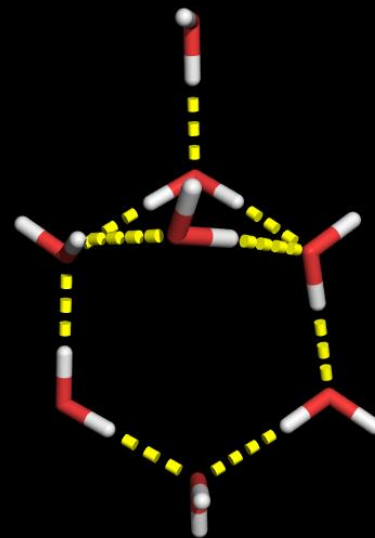
$$E_b = -0.590 \pm 0.070 \text{ eV}$$

## DFAAT



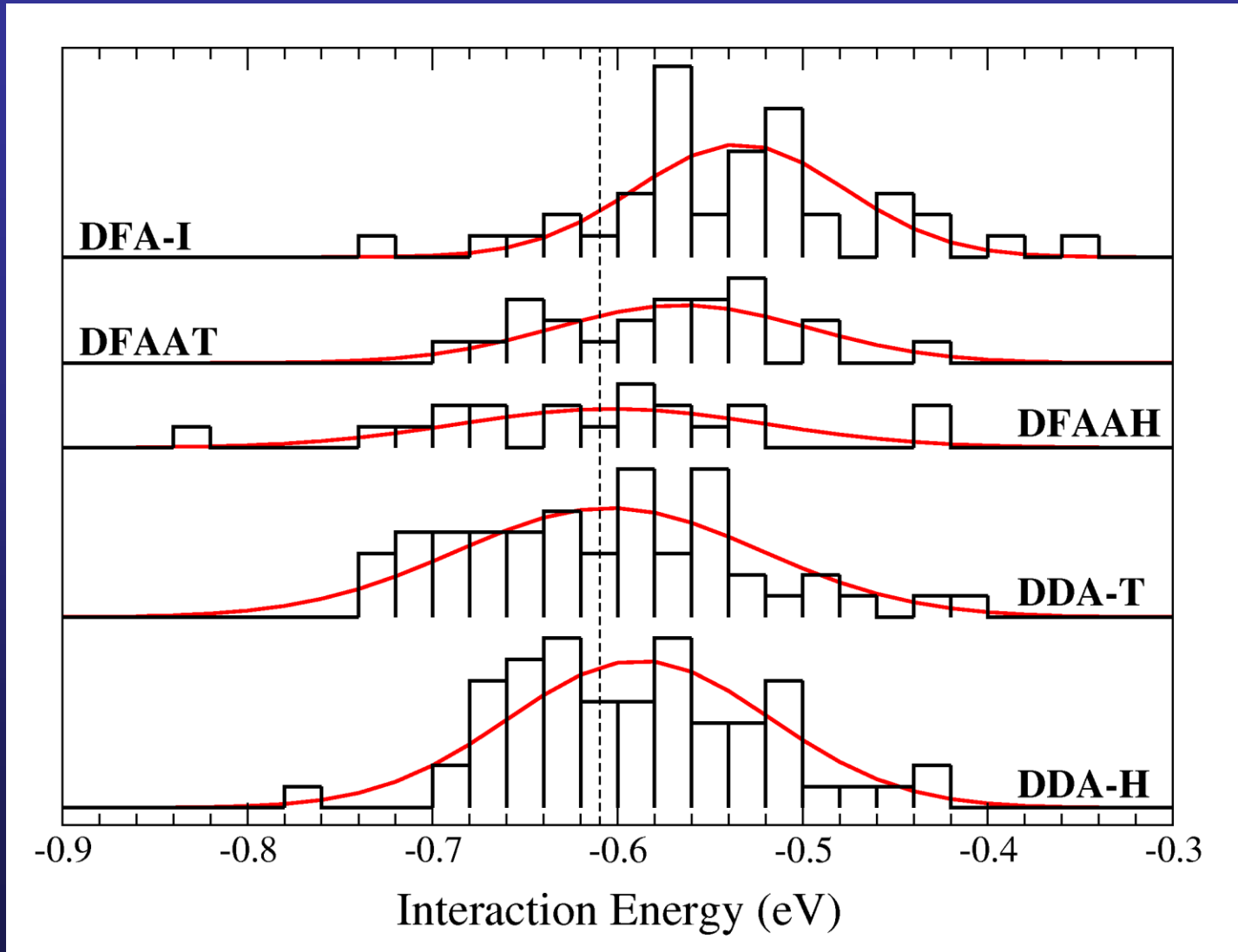
$$E_b = -0.578 \pm 0.066 \text{ eV}$$

## DFA-I

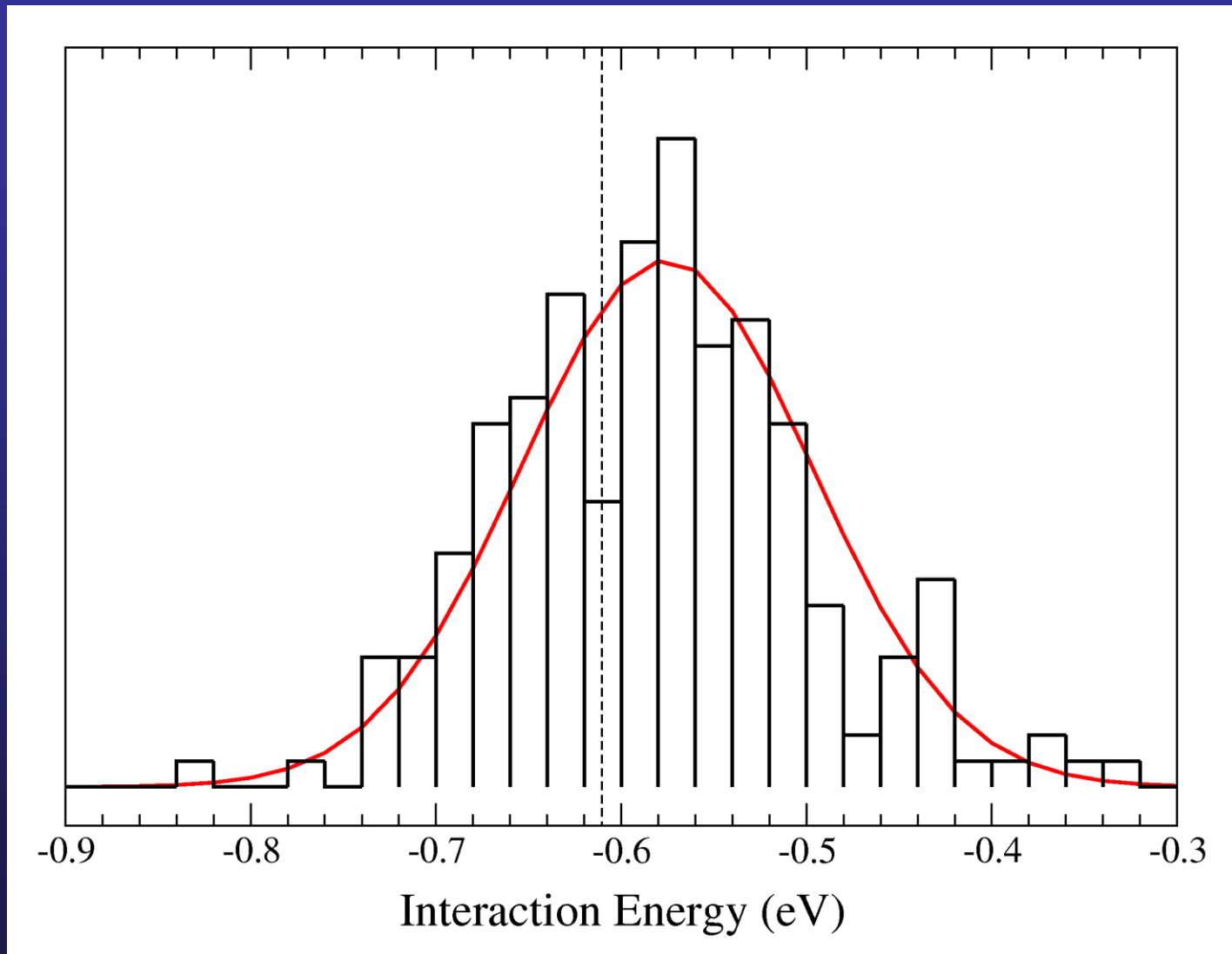


$$E_b = -0.539 \pm 0.074 \text{ eV}$$

# Energy histogram for each type of minima:



# Full histogram:



## Rounding up..

### **SCME:**

- **Good behavior over a wide range of conditions: water clusters, liquid water and bulk ice**
- **Fast**
- **Able to predict properties that were not included in the parametrization**

### **Adsorption:**

- **There are five prevalent types of sites for adsorption**
- **The distributions of the binding energies for each type of site are very similar**
- **Approximately 40% of the sites have a binding energy larger than the lattice energy of bulk ice Ih**

# Future

## **SCME:**

- Improved version of the potential that fixes some of the problems
- Faster coding and better software distribution

## **Adsorption:**

- Study of site-to-site transitions
- Use results to estimate surface diffusion rate
- Study multiple adsorptions/surface interactions

## **“Pet” project:**

- Modeling of the surface acoustic phonon modes
- Use results to estimate surface diffusion rate
- Study multiple adsorptions/surface interactions